

# Causality: Approaches and Pitfalls

Emily Oster

February 26, 2016

# The Problem

- Consider an outcome  $Y$ , treatment  $T$ , covariate vector  $X$ 
  - Example: job training on wages, low fat diet on heart disease, etc.
  - $y_{i1}$ : outcome for person  $i$  if they get  $T = 1$
  - $y_{i0}$  : outcome for person  $i$  if they get  $T = 0$
- What is the impact of T on Y?
- Object of Interest

$$E(y_{i1} - y_{i0})$$

# The Problem

- Observe  $y_{i1}$  or  $y_{i0}$  for a given person
  - You cannot see the same person at the same moment with and without the treatment

- What can you see?

$$\bar{y}_1 - \bar{y}_0$$

- What is the problem?
  - People with  $T = 1$  may be systematically different from those with  $T = 0$
- How can we figure out the causal impact of  $T$ ?

# Example and Outline

- Does eating a low fat diet lower your risk of mortality?
  - Y: Did you die?
  - T: Did you eat a low fat diet?
  - X: Other stuff about you
- Gold Standard
- Options with no special data requirements
- Options with special data requirements

- Randomized Controlled Trial
- How to do?
  - Recruit people
  - Randomly tell half of them to eat a low fat diet
  - Follow over time, observe mortality
  - Compare mortality in treatment, control groups
- Why does this work?
- Downsides: expensive, hard to do.

# Options with Common Data

- Example: NHANES Data
  - Dietary information
  - Good demographic data (education, income, etc)
  - Other health data
  - Can link to later mortality
- Selection on observables
- Selection on unobservables

# Selection on Observables

- Consider:

$$E(y_{i1}|T = 1, X_i) - E(y_{i0}|T = 0, X_i)$$

- i.e. a regression of  $Y$  on  $T$  which controls for observed covariates  $X$
- Uncovers causal effect if  $T$  is random conditional on  $X$
- In example:  $T$  diet,  $X$  education, income, race, age, gender.
- Pitfalls?

## Selection on Unobservables

- There are controls we are important in determining treatment which we do not observe
  - Without further assumptions, can say nothing
- Assume relationship between  $X$  and  $T$  is informative about relationship between  $T$  and unobserved variables  $W$
- May be able to bound effect size.

- These techniques can work with limited data requirements
- It is easy to look for heterogeneity across people
- Very transparent
- May not (probably does not) generate causal effect.
- Very difficult to figure out how far you are from causal.

# “Special” Data Techniques

- Imagine some variable  $Z$  which (randomly) pushes some people into treatment.
- Imagine isolating variation in treatment which is due to variation in  $Z$
- Use that part of the variation to estimate the impact of  $T$
- Examples:
  - Regression discontinuity
  - Instrumental Variables
  - Propensity Score

# Regression Discontinuity

- (Fake) Example.
- Doctors adopt new rule: BMI over 25, told to go on low-fat diet. BMI under 25, not told.
- Two individuals
  - BMI 24.9: Not told to go on low-fat diet
  - BMI 25.1: Told to go on low fat diet
- Otherwise similar (before/after breakfast)
- “Random” determination of diet advice
- If anyone listens to diet advice, can use this
  - Graph

# Regression Discontinuity: Minuses

- Effects are specific to the characteristics off of which you estimate them
  - What if low fat diet matters more if you are at a BMI of 40?
- Very strong data requirements
- Must be sure other things do not vary across the threshold
  - Why did they put the rule there in the first place?

# Instrumental Variables

- (Fake) Example.
- Religion  $Z$  requires being a vegetarian; on average, vegetarians eat less fat
  - Key assumption (“exclusion restriction”): religion does not otherwise affect mortality
- Relate  $Z$  to  $T$ , calculate  $\hat{T}$
- Relate  $Y$  to  $\hat{T}$ 
  - Effect is driven only by the variation in  $T$  that is driven by  $Z$ .
  - $Z$  only impacts  $Y$  through  $T$ .

# Instrumental Variables: Minuses

- Effects local to people impacted by the instrument
- Stringent data requirements
  - Exclusion restriction often implausible.

# Propensity Score

- I know full set of variables that determine  $T$ . Actual  $T$  contains some random-ness.
- I do not know how variables enter to determine  $T$ 
  - polynomials, interactions, etc
- Entering all variables in regression over fits
- Generate  $Pr(T)$  by regressing  $T$  on all variables and combinations and predicting
  - Note on LASSO
- Control for  $Pr(T)$ ,  $T$ .
- Pitfalls

# Final Thoughts

- Causality is hard to show.
- Tension between strength of causality and locality of effect.
- I am in some ways more bullish than most on the first set of things,
  - Especially in the era of big data.