



AI Research for Climate Change and Environmental Sustainability

Claire Monteleoni



University of Colorado
Boulder



December 2021: Boulder County, Colorado

- Snow drought conditions through fall and winter 2021 created dry land-cover
- 80-100 mph winds, combined with ignition, launched an uncontrollable “fire storm”
- Loss of 2 lives. 1000 homes and 20 businesses were destroyed, and more damaged

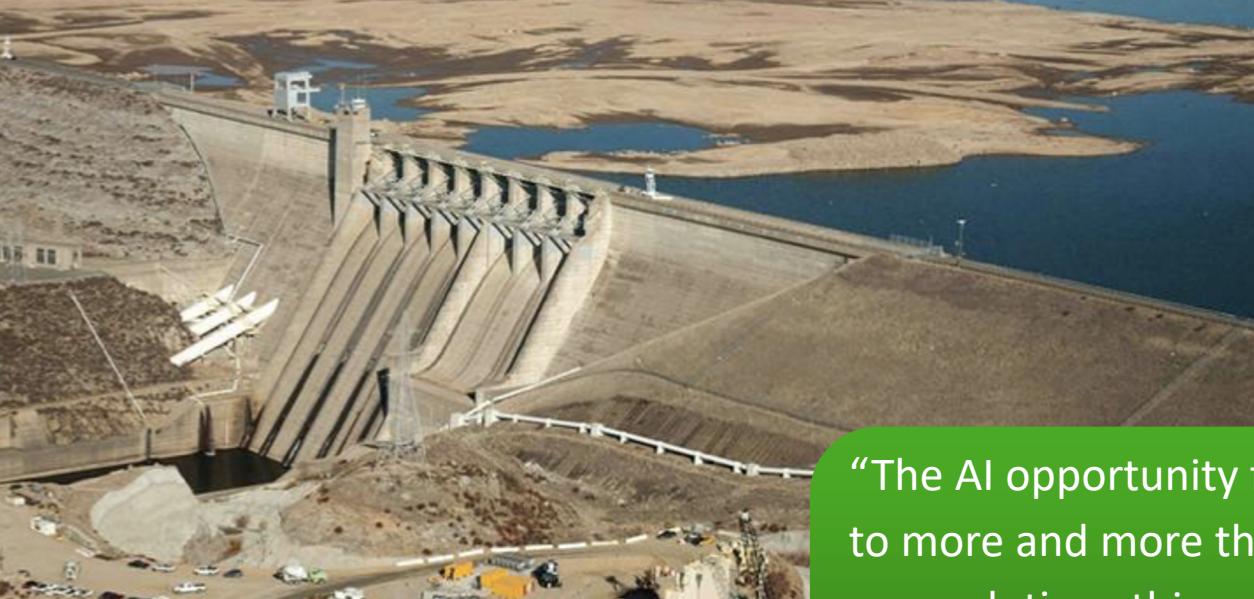


January 2018: Montecito, Santa Barbara County

- Thomas Fire destroyed 1063 structures and led to poor air quality
- Intense rainfall as the fire was nearing containment produced a debris flow
- 23 lives and over 130 homes were lost
- Damage to critical transportation and water resource infrastructure



Machine learning can shed light on climate change



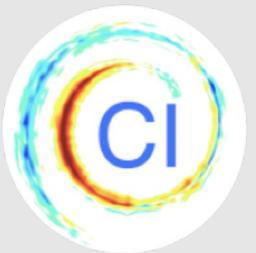
“The AI opportunity for the Earth is significant. Today’s AI explosion will see us add AI to more and more things every year.... As we think about the gains, efficiencies and new solutions this creates for nations, business and for everyday life, we must also think about how to maximize the gains for society and our environment at large.”

– The World Economic Forum: Harnessing Artificial Intelligence for the Earth. 2018



Climate Informatics is based on the vision that Machine learning can shed light on climate change

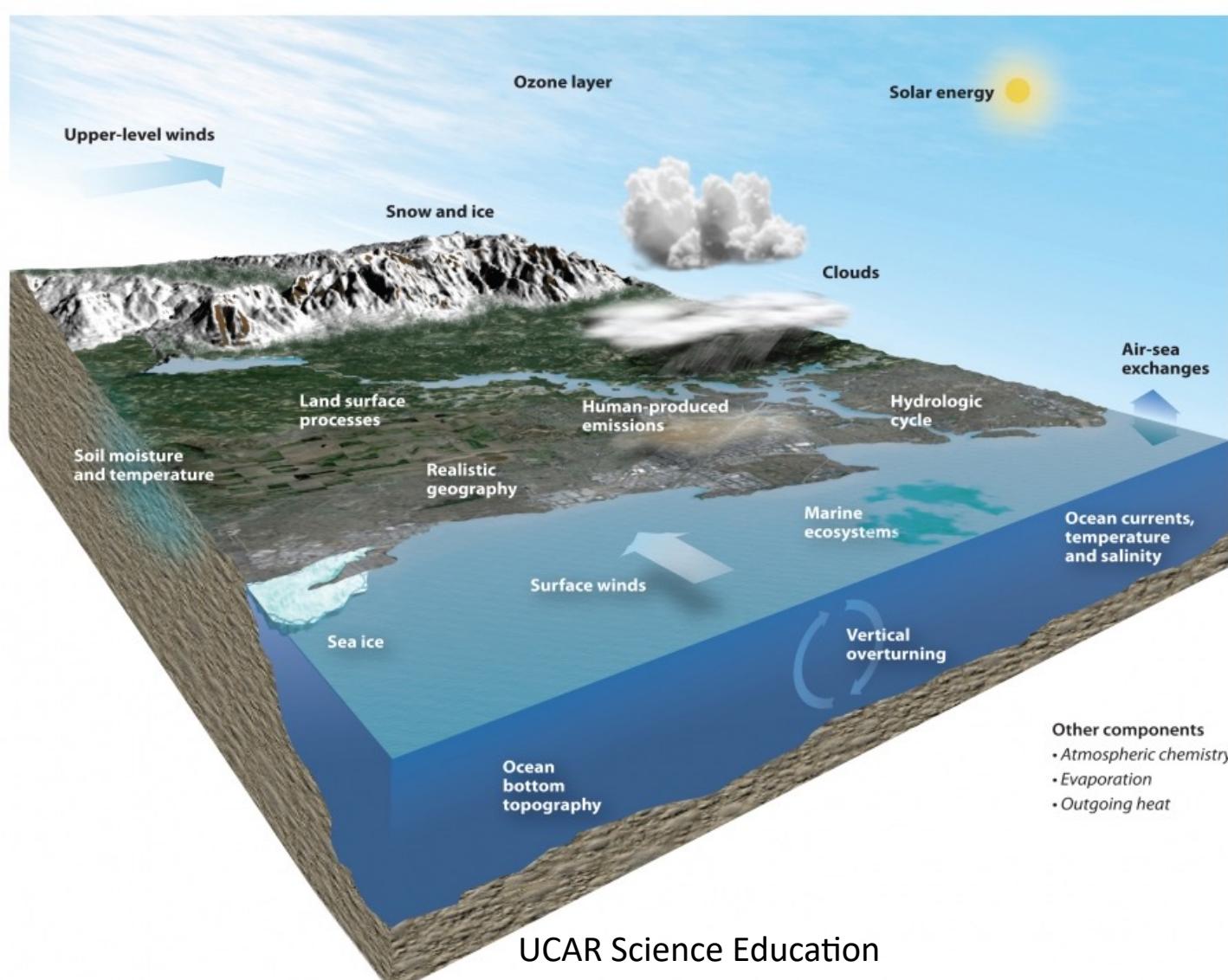
- 2008 Start work on Climate Informatics (with Gavin Schmidt, NASA)
- 2010 “Tracking Climate Models” [Monteleoni et al., NASA CIDU, Best Paper]
- 2011 Launch of International Conference on Climate Informatics, NYAS
- 2013 “Climate Informatics” book chapter [M et al., SAM]
- 2014 "Climate Change: Challenges for Machine Learning," [M & Banerjee, NeurIPS]
- 2015 Launch of Climate Informatics Hackathon, Paris and Boulder, CO
- 2018 World Economic Forum recognizes Climate Informatics as key priority
- 2019 Climate Informatics Conference held at ENS, Paris
- 2022 First batch of articles published in Environmental Data Science,
Cambridge University Press
- 2022 11th Conference on Climate Informatics and 8th Hackathon, NOAA, North Carolina
- 2023 12th Conference on Climate Informatics and 9th Hackathon, Cambridge UK, April



AI for Climate Change and Environmental Sustainability

- Understanding and Predicting Climate Change: Ocean, Atmosphere, and Water-cycle
- AI-driven Forecasting of Extreme Weather and Cascading Hazards
- AI for Green Energy and Industry

Understanding and Predicting Climate Change: Ocean, Atmosphere, and Water-cycle



Online learning from non-stationary spatiotemporal data to adaptively combine climate model ensemble forecasts

[Multiple papers 2009-2020, e.g., AAAI 2012, ALT 2020]

Causal information hubs in Pacific ENSO region

[Saha et al. Climate Informatics 2019]

NASA project to attribute and forecast sea-level rise using climate models and satellite altimetry

Online learning with spatiotemporal non-stationarity

Learning when the target concept can **vary over time**,
and **multiple other dimensions** (e.g., latitude, longitude)

We can **exploit local structure in space and time**

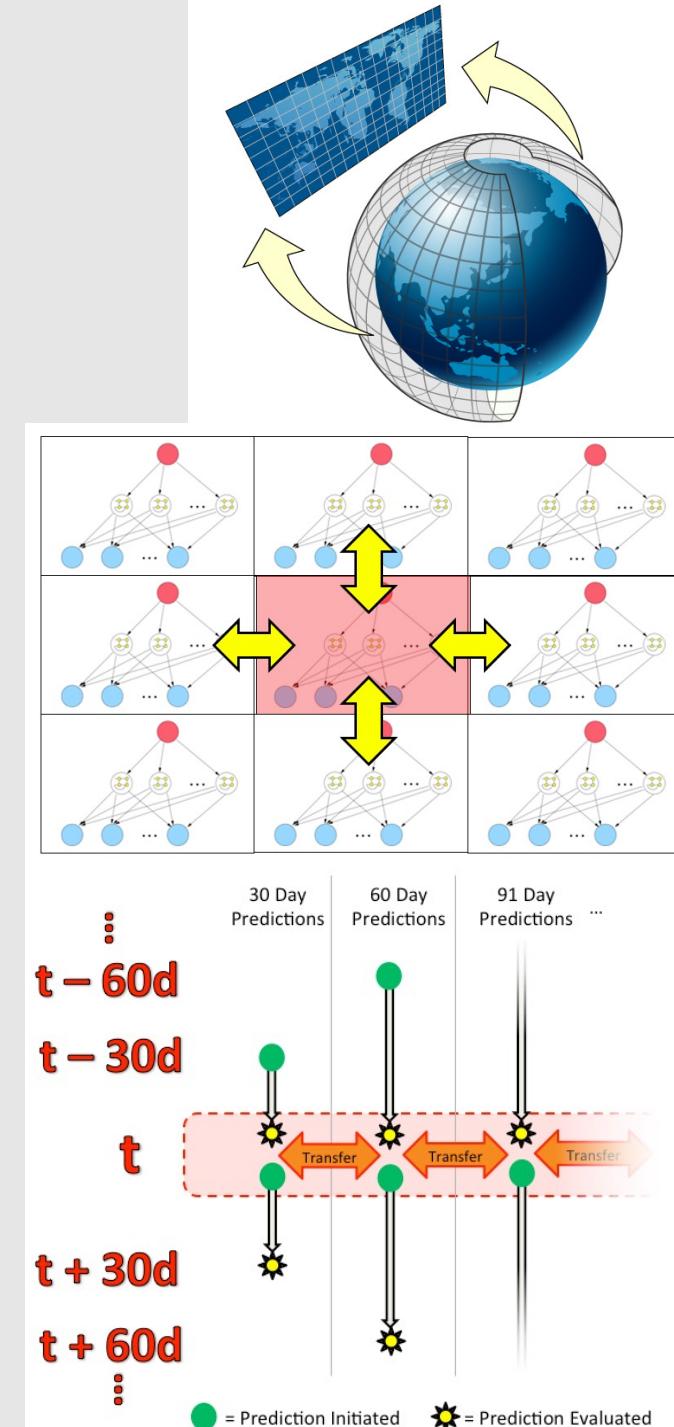
We can **learn the level of non-stationarity in time and space**

[McQuade and Monteleoni, AAAI 2012] extended [Monteleoni & Jaakkola,
NeurIPS 2003; Monteleoni et al. SAM 2011] to **multiple dimensions**

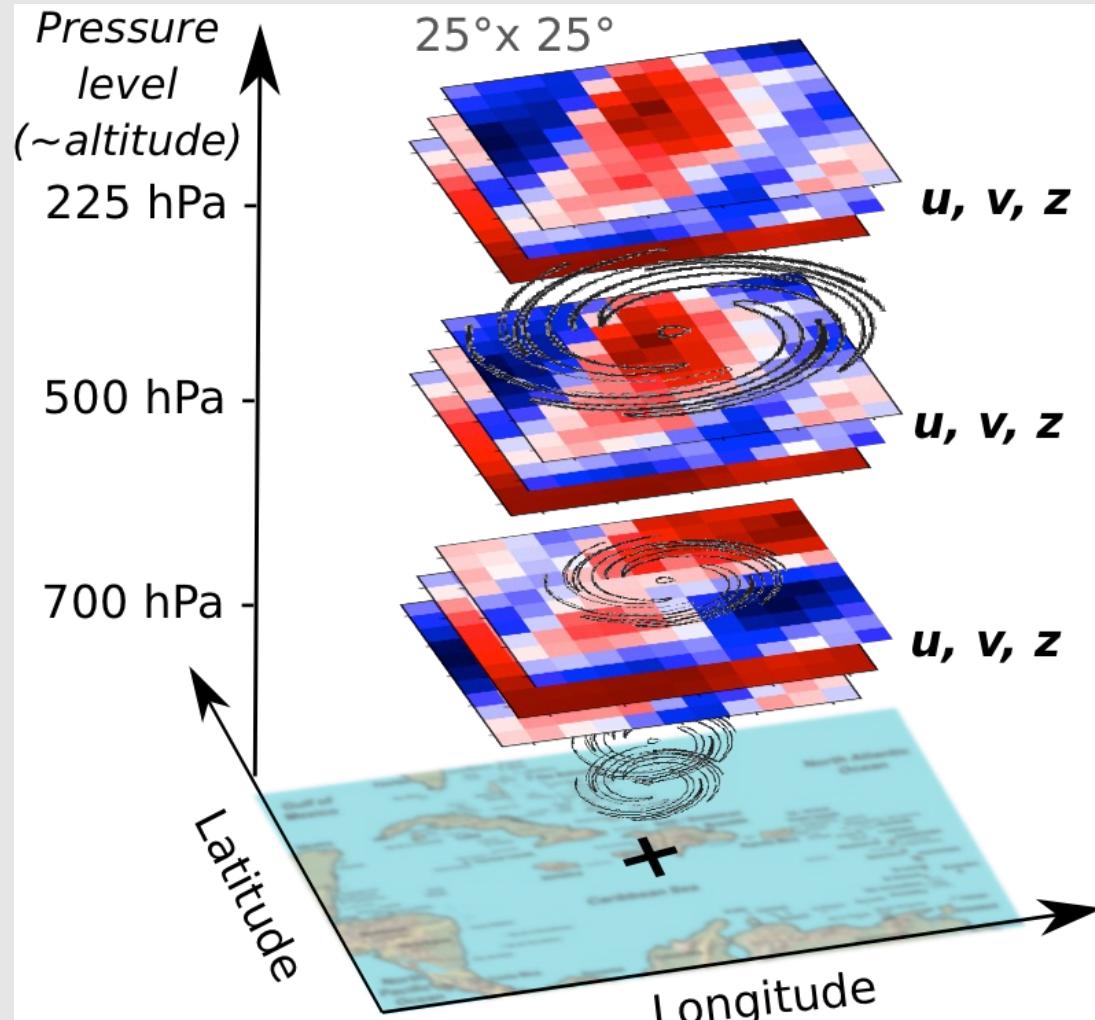
This framework for online learning was **open in machine learning**
New “regret” framework: [Cesa-Bianchi, Cesari, & Monteleoni, ALT 2020]

Prediction at **multiple timescales simultaneously**

Applications to both climate science, and financial volatility:
[McQuade and Monteleoni, CI 2015; SIGMOD DSMM 2016]



AI-driven Forecasting of Extreme Weather and Cascading Hazards



Defining and detecting diverse, multivariate extreme events with topic modeling

[Tang & Monteleoni, Climate Informatics 2014; IEEE CISE 2015]

Hurricane track prediction via fused CNNs

[Giffard-Roisin et al., Climate Informatics 2018; Frontiers 2020]

Avalanche detection using CNN; VAE

[Sinha et al., Climate Informatics 2019; 2020] with Météo-France

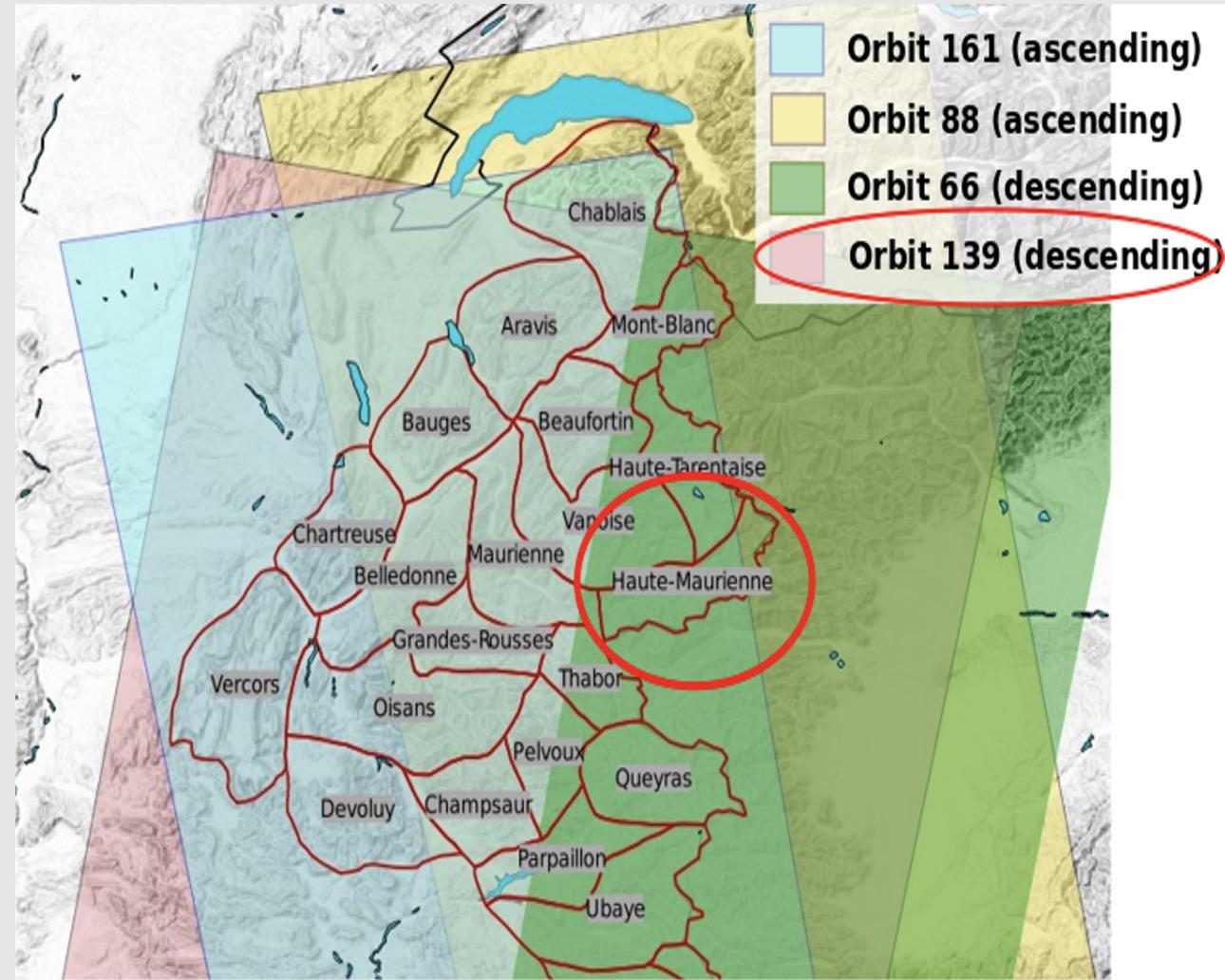
Forecasting Indian Summer Monsoon precipitation extremes

[Saha et al. Climate Informatics 2019; 2020] with India Meteo. Dept.

Avalanche detection

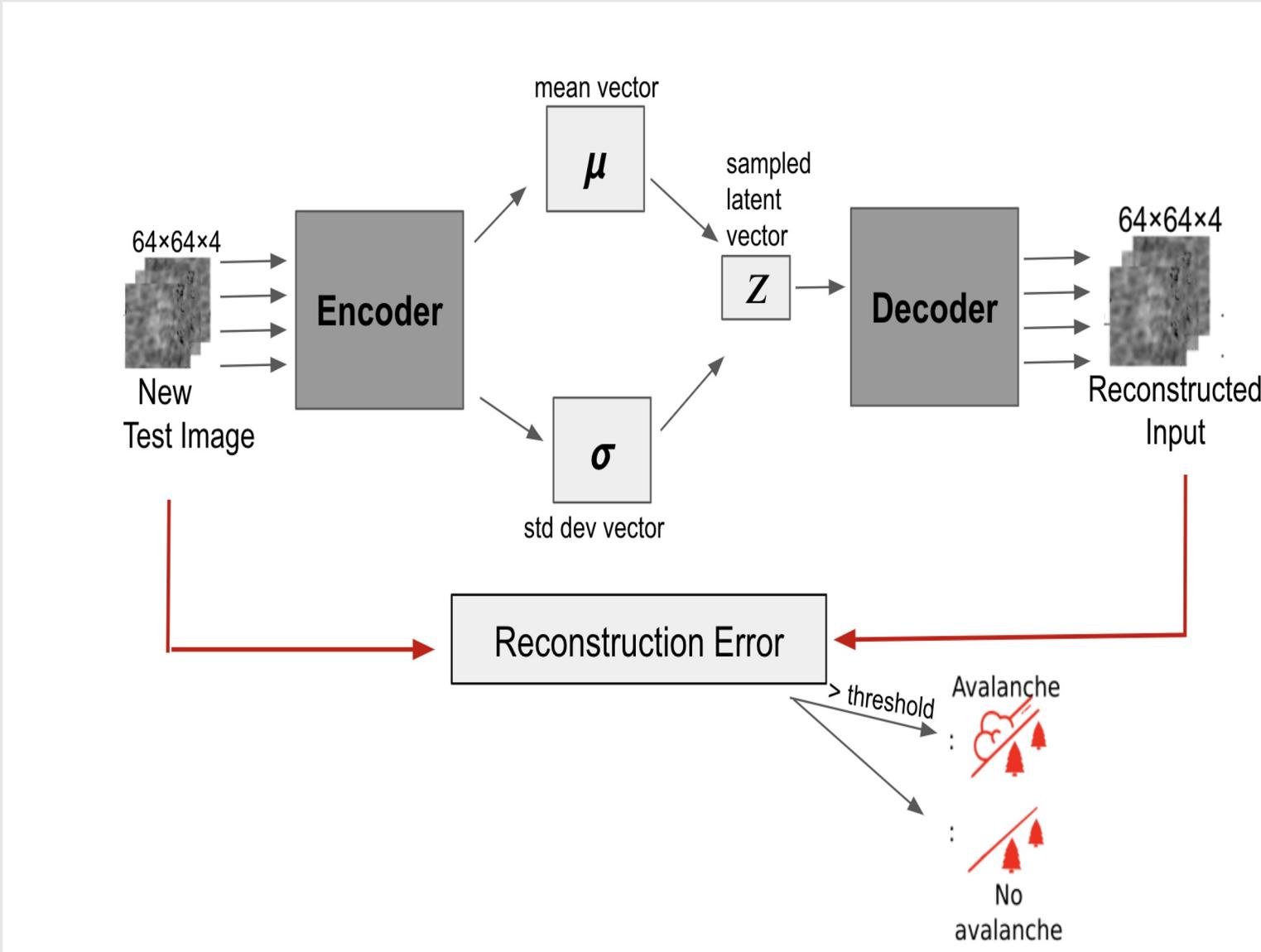
[Sinha et al., Climate Informatics 2020]

- **Limited** in-situ ground-truth measurements
 - Météo-France
- **Unlabeled** SAR imagery
 - Monitoring French Alps in 2017-2018
 - Sentinel-1A and 1B satellites
 - 4 features:
 - Backscatter coefficients at present and previous time
 - Topological features: Slope & Angle



METEO
FRANCE

Avalanche detection using VAE anomaly detection





AI for Green Energy and Industry

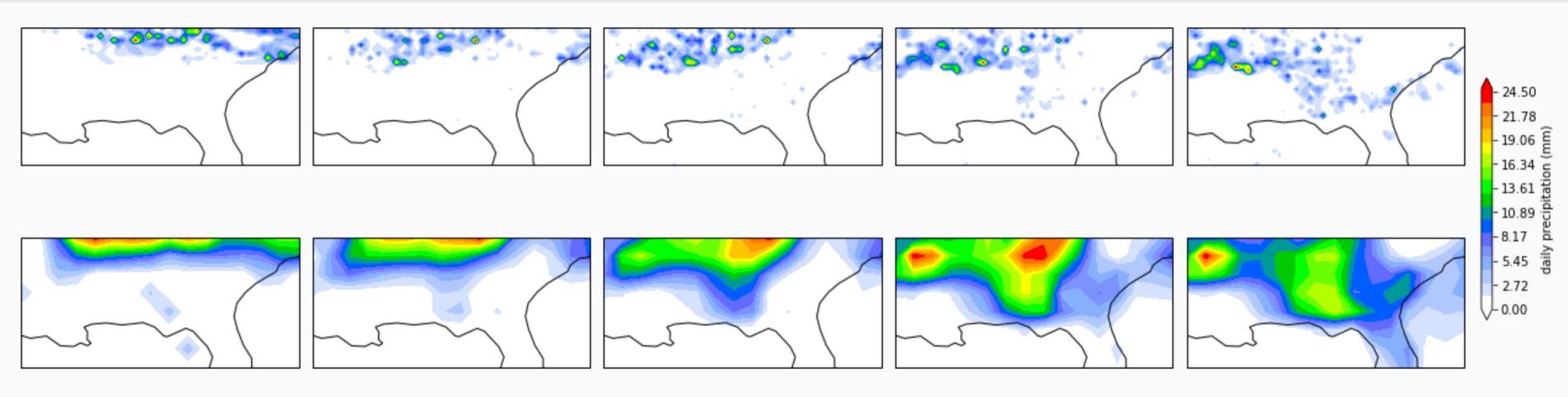
Week-ahead solar irradiance
forecasting via deep sequence
learning

[Sinha et al., CI 2022] with NREL

CCAI / Future Earth project to
downscale climate model data
for renewable energy planning
in U.S. and India

[Harilal et al., NeurIPS workshop 2022]

ClimAlign: Unsupervised, generative downscaling



[Groenke et al., CI 2020]

General downscaling technique via domain alignment with normalizing flows
[AlignFlow: Grover et al., AAAI 2020][Glow: Kingma & Dhariwal, NeurIPS 2018]

- **Unsupervised**: do not need paired maps at low and high resolution
- **Generative**: can sample from posterior over latent representation OR sample conditioned on a low (or high!) resolution map
- **Interpretable**, e.g., via interpolation

Our Climate Informatics research also addresses open problems in Machine Learning

- Online learning with spatiotemporal non-stationarity
- Prediction at multiple timescales simultaneously
- Anomaly detection with limited supervision
- Tracking highly-deformable patterns

Challenges/Bottlenecks in Climate Informatics

Data limitations

- Limited labeled data: unsupervised learning, dimensionality reduction
- Class imbalance: e.g., extreme events are rare by definition!
- Data is limited along the time dimension. **Can we substitute data diversity and granularity over space?**

Scale resolution challenges

- Downscaling spatiotemporal data fields
- Climate model parameterization problems

Non-stationarity

- Climate *change* means we cannot assume i.i.d. data!
- ML models need to adapt over time, and space

Interpretability

- Evaluation of generative models is an active research area of core ML

Environmental Data Science Innovation & Inclusion Lab

A national accelerator linking data, discovery, & decisions



NSF's newest data synthesis center,
hosted by the University of Colorado Boulder & CIRES,
with key partners CyVerse & the University of Oslo





ENVIRONMENTAL DATA SCIENCE

An interdisciplinary, open access journal dedicated to the potential of artificial intelligence and data science to enhance our understanding of the environment, and to address climate change.

Data and methodological scope: Data Science broadly defined, including:

Machine Learning; Artificial Intelligence; Statistics; Data Mining; Computer Vision; Econometrics

Environmental scope, includes:

Water cycle, atmospheric science (including air quality, climatology, meteorology, atmospheric chemistry & physics, paleoclimatology)

Climate change (including carbon cycle, transportation, energy, and policy)

Sustainability and renewable energy (the interaction between human processes and ecosystems, including resource management, transportation, land use, agriculture and food)

Biosphere (including ecology, hydrology, oceanography, glaciology, soil science)

Societal impacts (including forecasting, mitigation, and adaptation, for environmental extremes and hazards)

Environmental policy and economics

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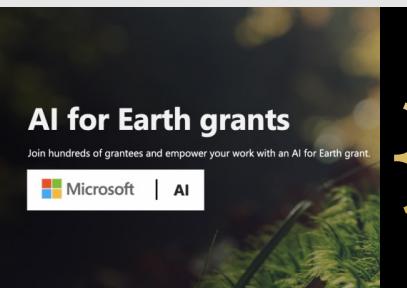
Climate and Machine Learning
Boulder (CLIMB)



Thank you!

And many thanks to:

Arindam Banerjee, *University of Illinois Urbana-Champaign*
Nicolò Cesa-Bianchi, *Università degli Studi di Milano*
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Guillaume Charpiat, *INRIA-Saclay*
Cécile Coléou, *Météo-France & CNRS*
Michael Dechartre, *Irstea, Université Grenoble Alpes*
Nicolas Eckert, *Irstea, Université Grenoble Alpes*
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Brian Groenke, *Alfred Wegener Institute, Potsdam*
Tommi Jaakkola, *MIT*
Anna Karas, *Météo-France & CNRS*
Fatima Karbou, *Météo-France & CNRS*
Balázs Kégl, *Huawei Research & CNRS*
Luke Madaus, *Jupiter Intelligence*
Scott McQuade, *Amazon*
Ravi S. Nanjundiah, *Indian Institute of Tropical Meteorology*
Moumita Saha, *Philips Research India*
Gavin A. Schmidt, *NASA Senior Advisor on Climate*
Saumya Sinha, *University of Colorado Boulder*
Cheng Tang, *Amazon*



PhDs, postdocs, and positions available in Paris!

Inria Paris

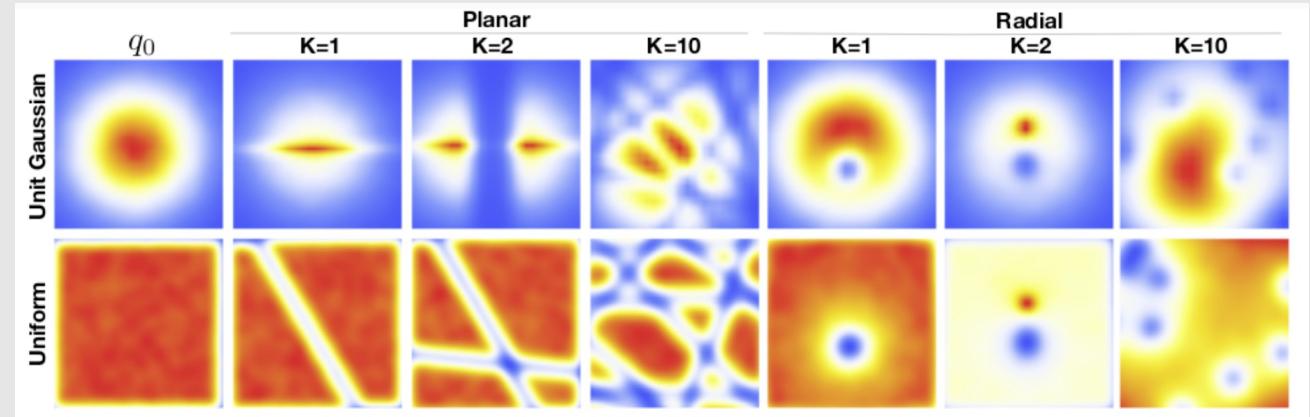
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Bonus slides

Normalizing Flows

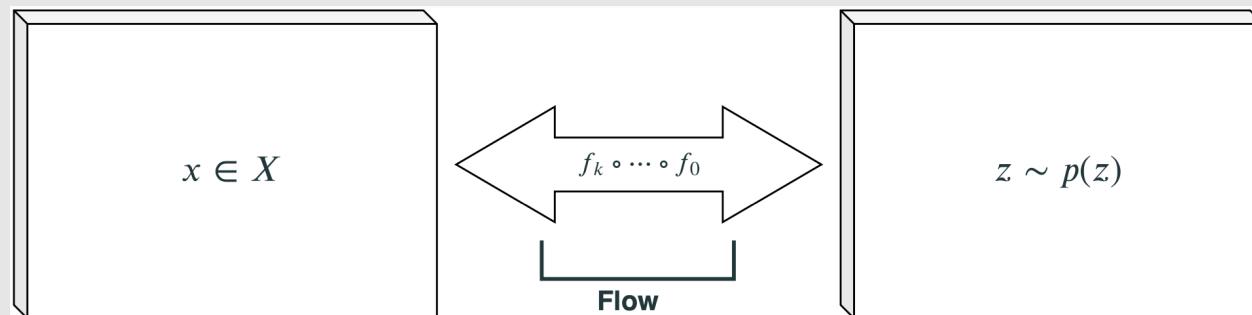
[Rezende & Mohamed, ICML 2015]



Can be viewed as extension of VAE beyond Gaussian assumption on latent space

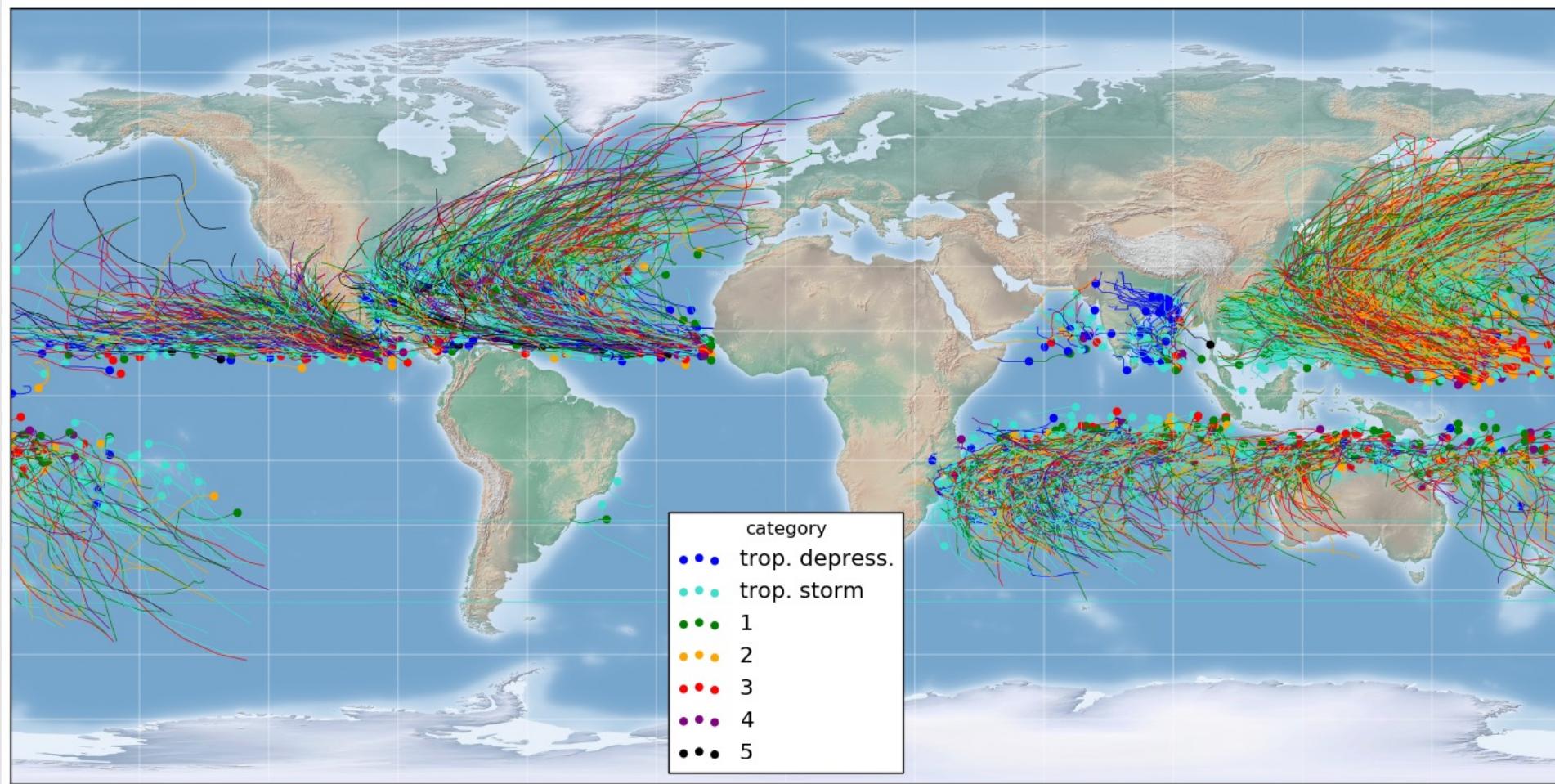
Learn a series of **invertible transformations**, $\{f_i\}$, from a simple prior on latent space, Z , to allow for more informative distributions on the latent space:

$$z_k = f_k \circ f_{k-1} \circ \cdots \circ f_1(z_0)$$



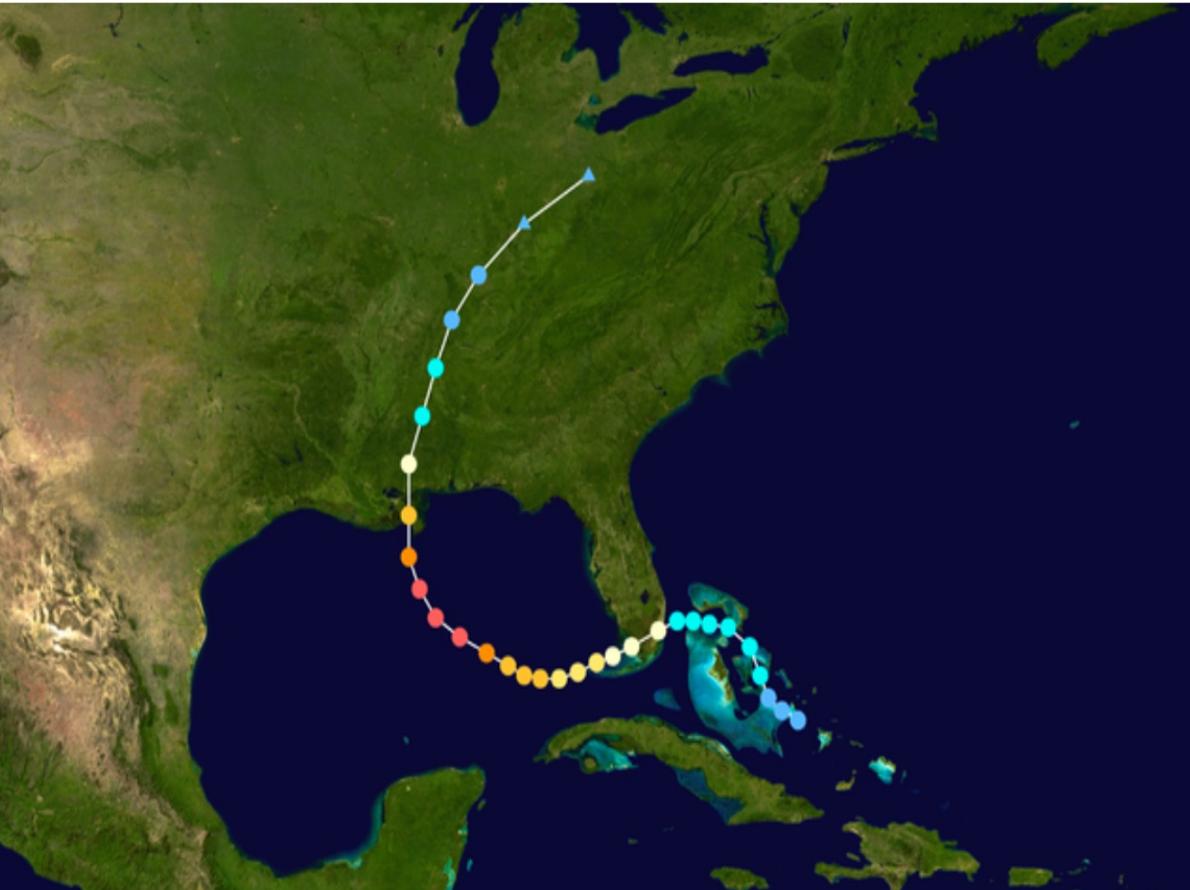
Storm track data

3000 tropical/extratropical storm tracks since 1979, measurements every 6 hrs



NOAA IBTrACS database

Storm track data

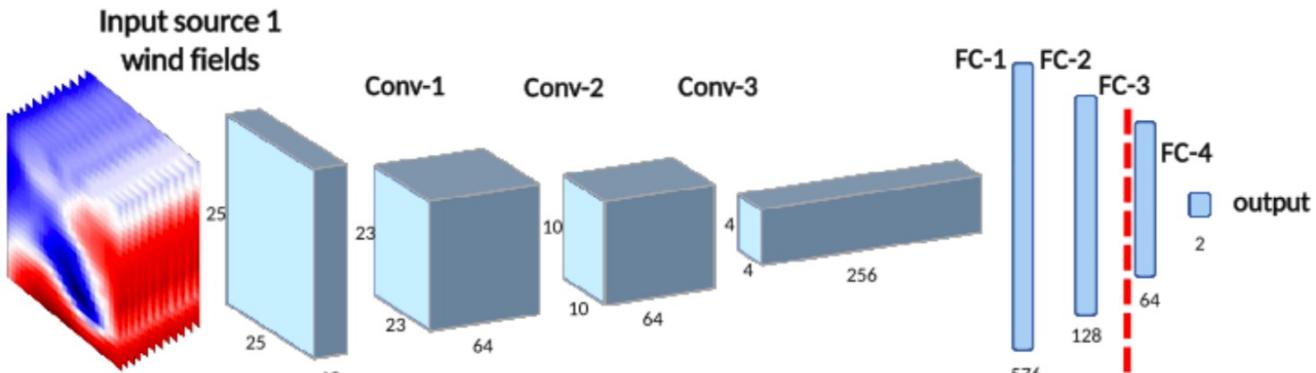


Saffir-Simpson Hurricane Scale		
Category	Wind Speed mph	Wind Speed knots
5	≥ 156	≥ 135
4	131-155	114-134
3	111-130	96-113
2	96-110	84-95
1	74-95	65-83
Non-Hurricane Scale		
Tropical Storm	39-73	34-64
Tropical Depression	0-38	0-33

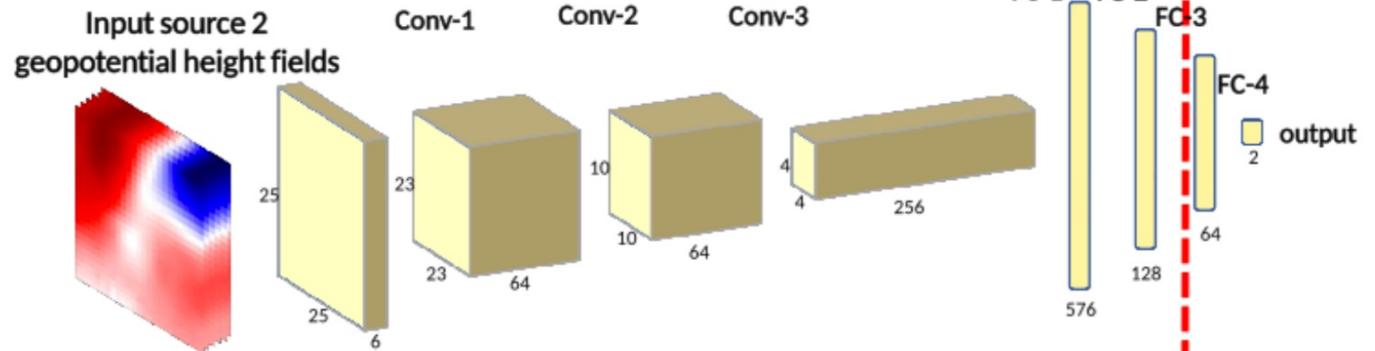
- Hurricane Katrina, 2005. (1 dot every 6 hours).
- **Tracks and Intensity** : Two main goals of the forecast

Deep Learning fusion network

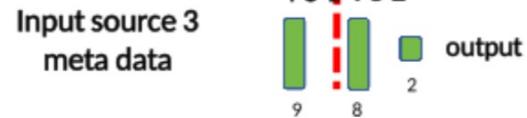
Wind CNN



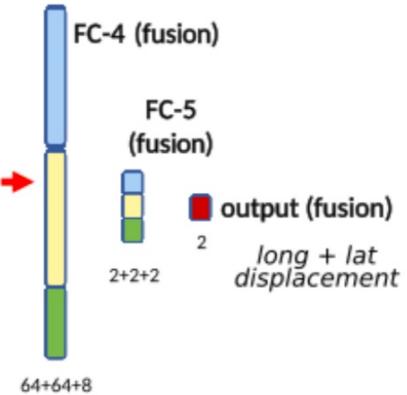
Pressure CNN



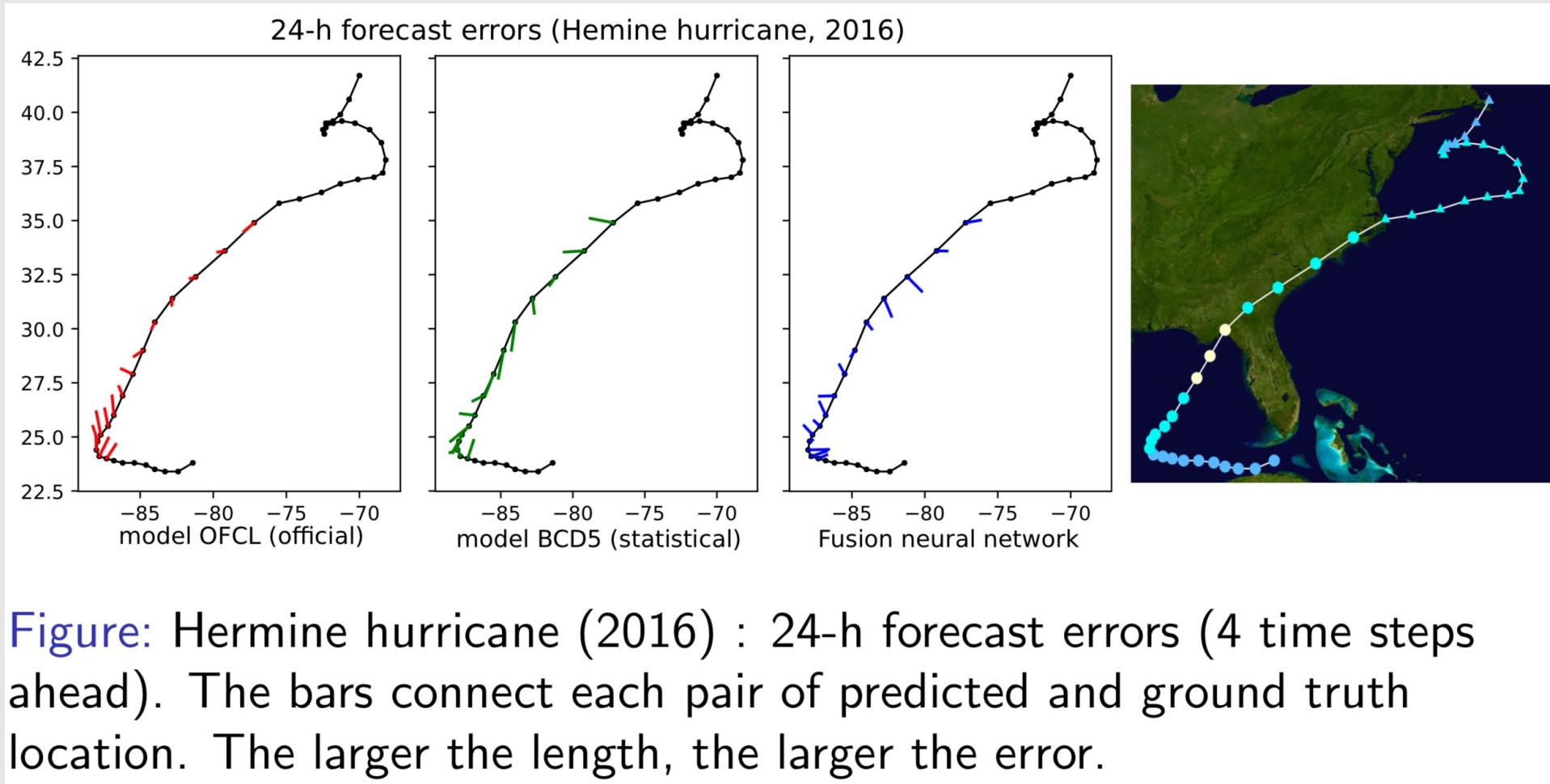
Past tracks + meta NN



Fusion Network

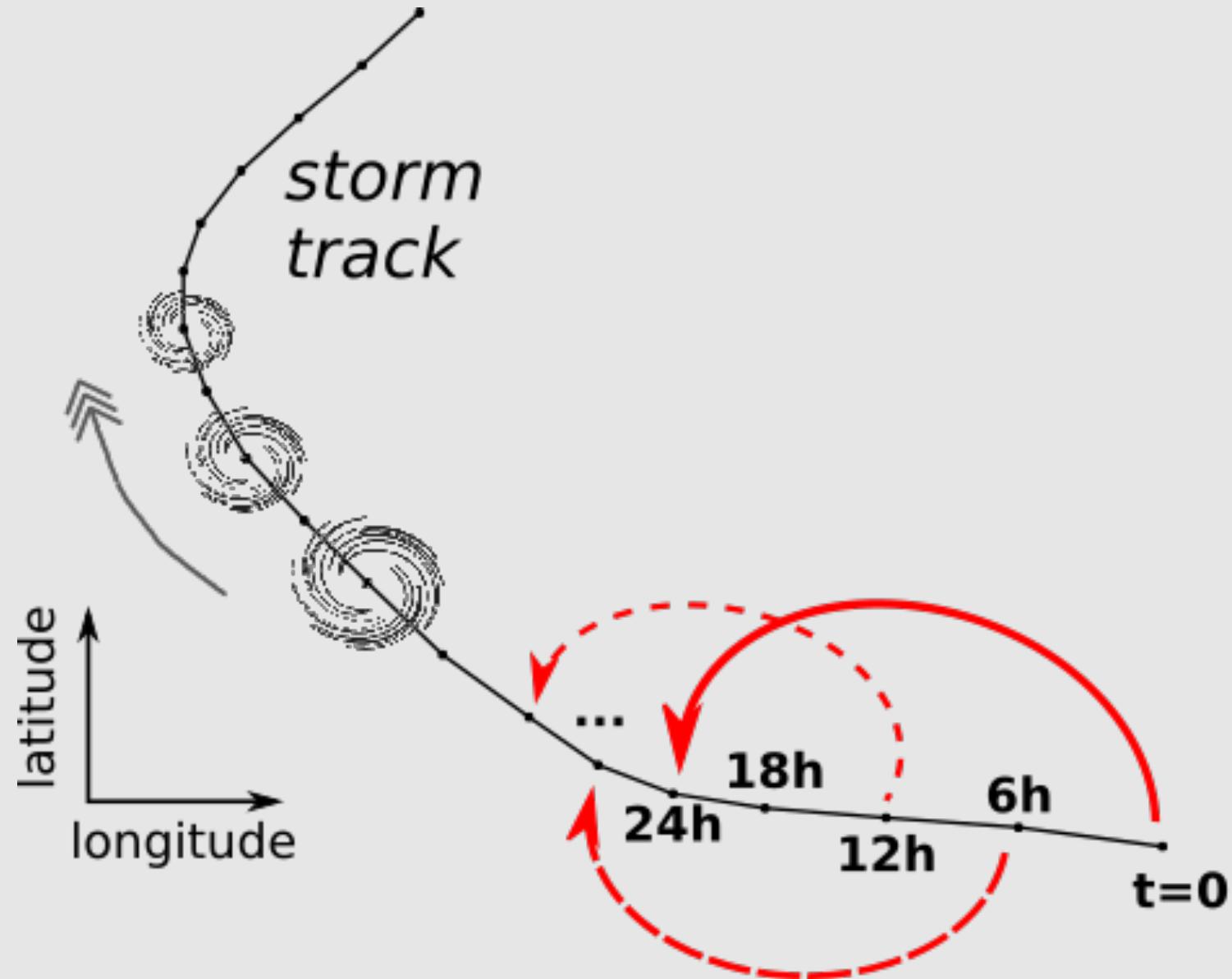


Comparison to benchmarks



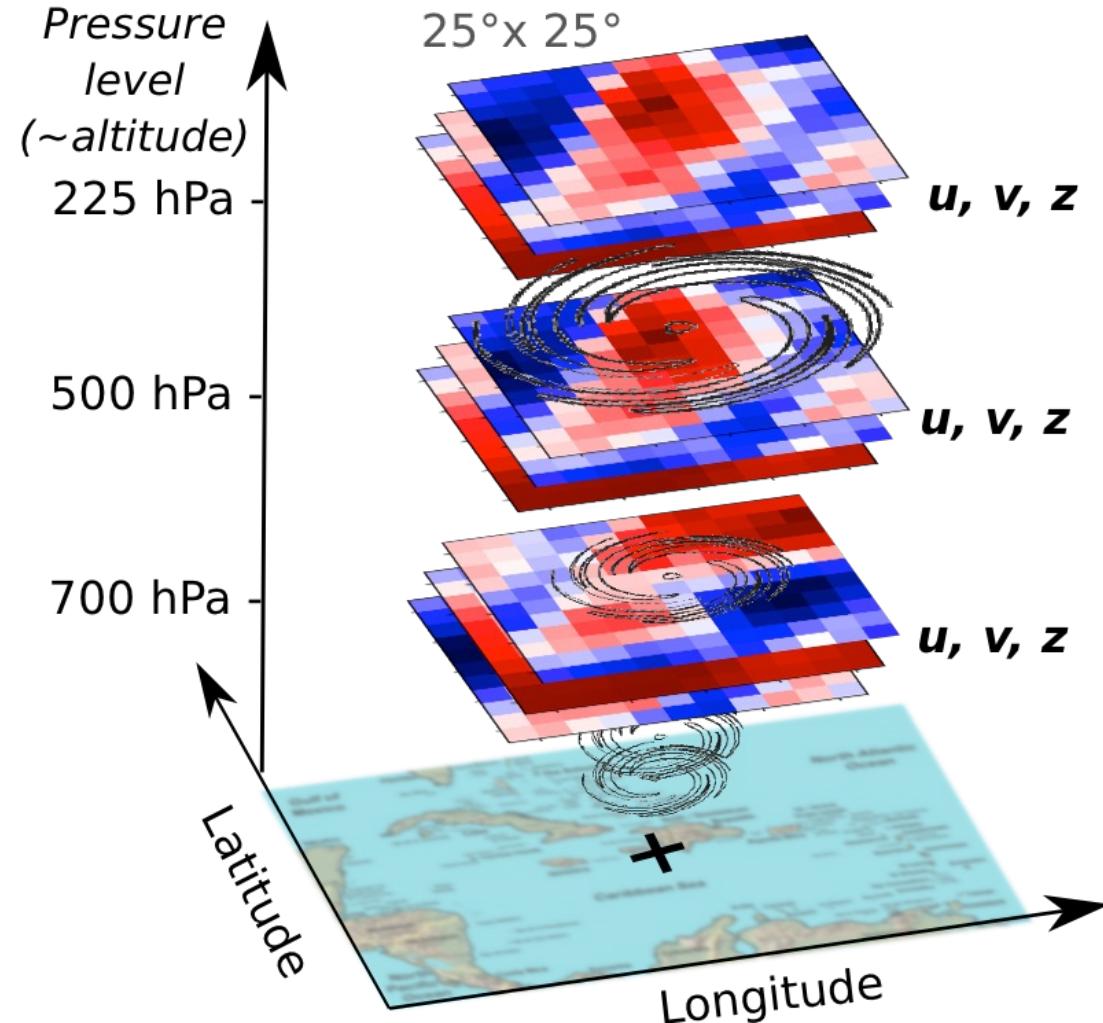
[Giffard-Roisin et al.,Frontiers 2020]

Forecasting task: 24h spatial displacement



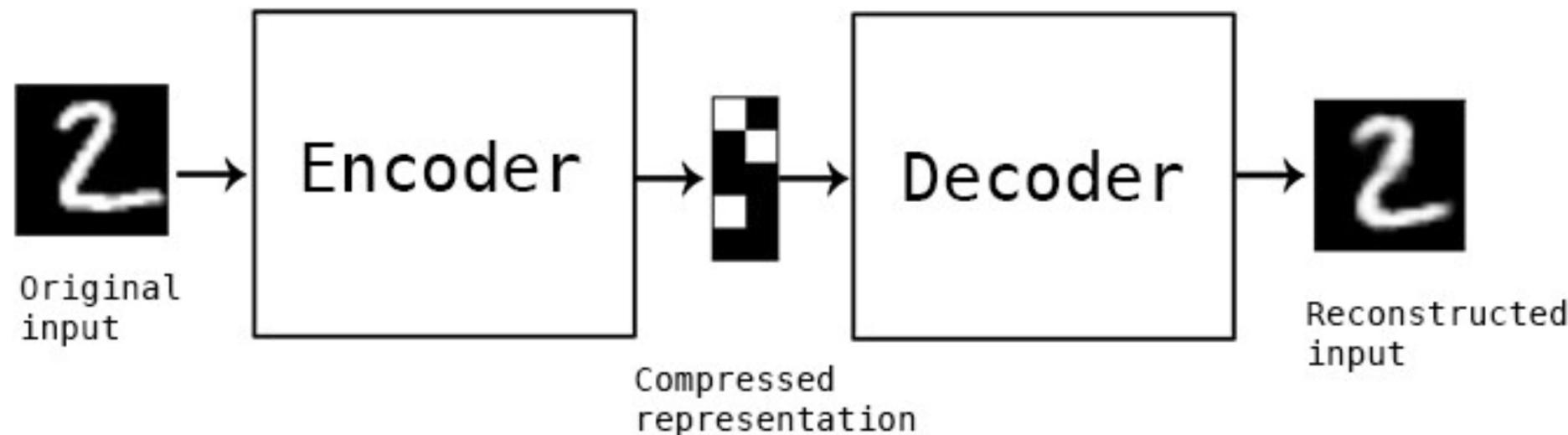
Our approach: moving frame-of-reference

- Estimate future **displacement** as $\vec{u} = (dx, dy)$
- Centered reanalysis data (center = current storm location)

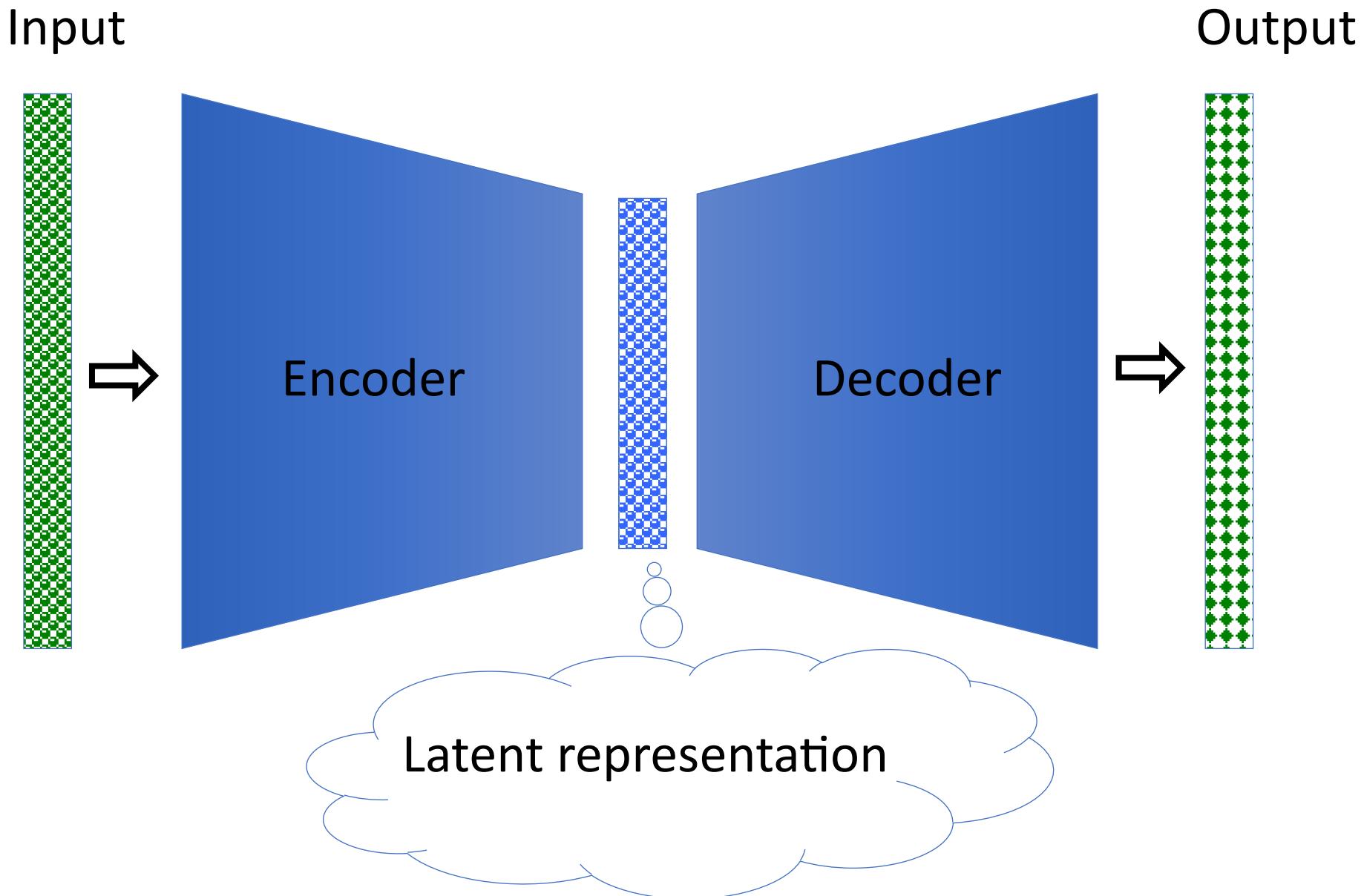


What is an Auto-encoder?

- Train a neural network in an **unsupervised** setting
 - Use the unlabeled data both as input, and to evaluate the output
- After training, the bottleneck layer will be a **compact representation** of the input distribution

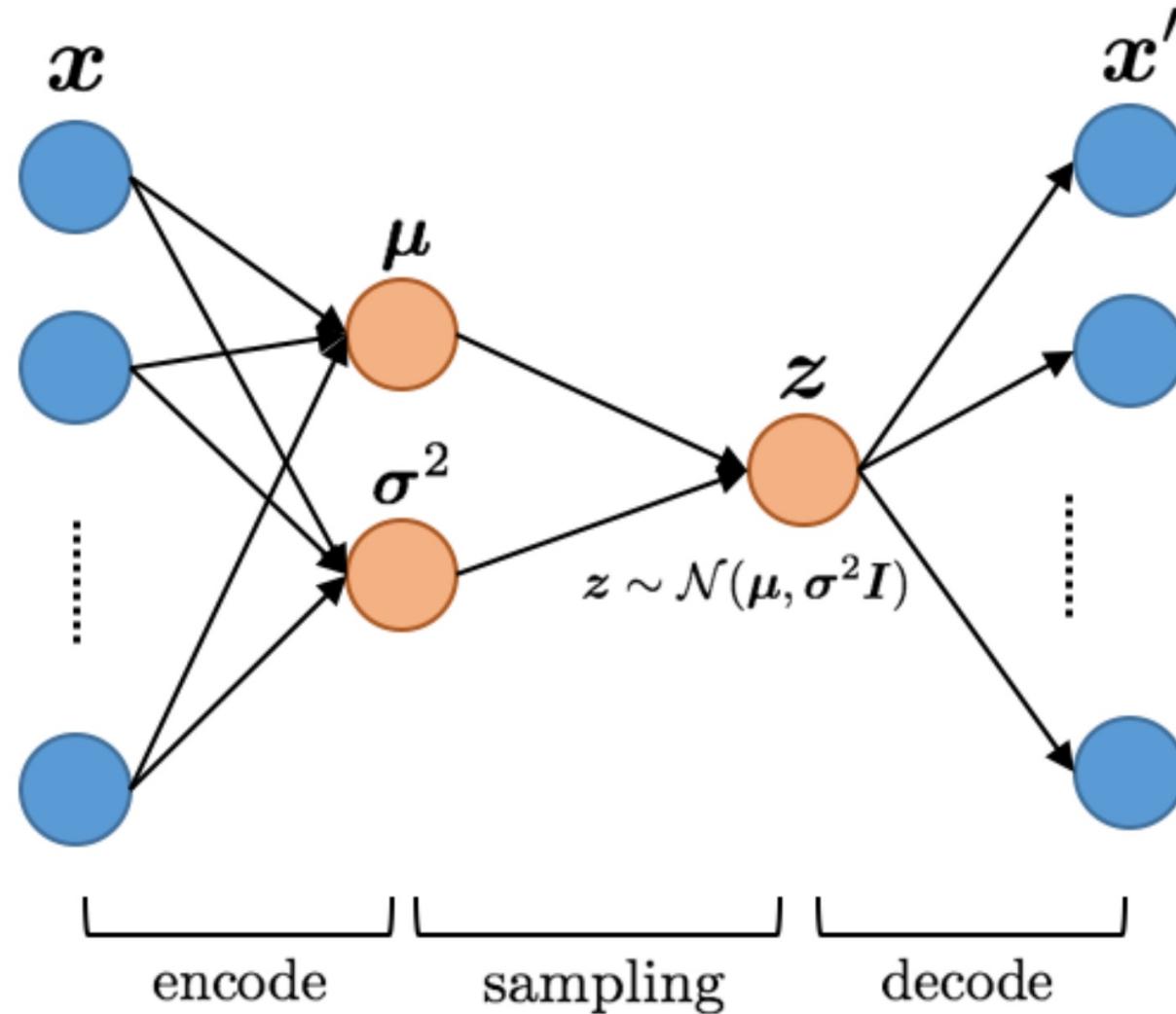


Autoencoder: The parameters of the encoder and decoder networks are trained to make the output approximate the input. After training on many input examples, the parameters of the bottleneck layer form a compact representation of the input distribution.



Variational Autoencoder (VAE)

Learn a **distribution** over latent representations (instead of a single encoding).



Unsupervised Deep Learning

- Supervised DL. Prediction loss is a function of the label, y , and the network's output on input x .

Network output

$$f_W(x) = \hat{y}$$

Loss function

$$\mathcal{L}(\hat{y}, y)$$

- Unsupervised DL. Prediction loss is only a function of x , and the network's output on input x . There is no label, y .

Network output

$$f_W(x) = \hat{x}$$

Loss function

$$\mathcal{L}(\hat{x}, x)$$

Downscaling as domain alignment

- Domain alignment task: given random variables X, Y , learn a mapping $f: X \rightarrow Y$ such that, for any $x_i \in X$ and $y_i \in Y$,

$$f(x_i) \sim P_Y \quad f^{-1}(y_i) \sim P_X$$

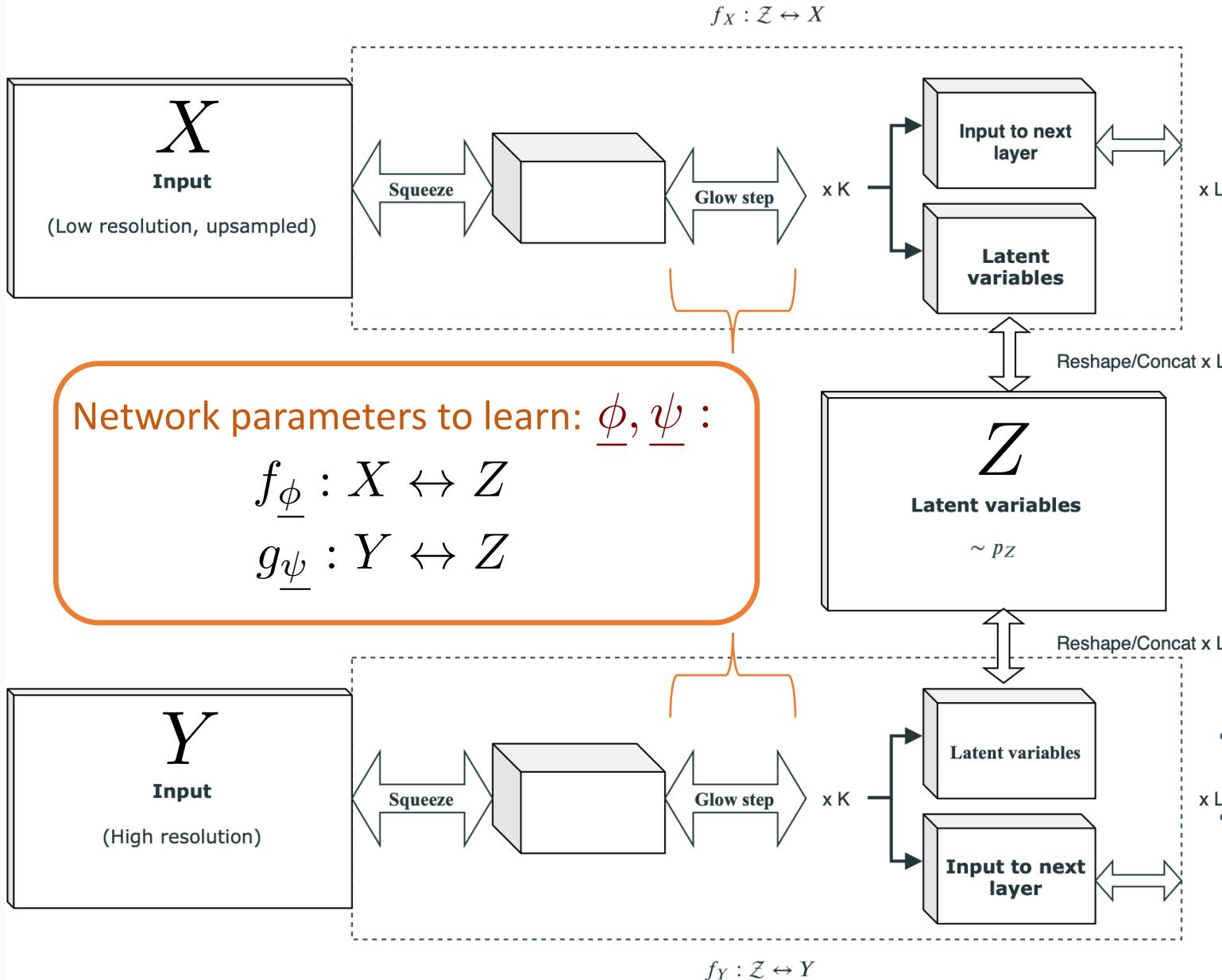
- **Downscaling as domain alignment**

- Learn the joint PDF over X and Y , by assuming conditional independence over a shared latent space Z

$$P_{XY}(x, y) = \int_{z \in Z} P_{XYZ}(x, y, z) dz = \int_{z \in Z} P(x|z)P(y|z)P_Z(z) dz$$

- Model $P(x|z), P(y|z)$ using AlignFlow [Grover et al. 2020]
- Starting with a simple prior on P_Z , learn normalizing flows
- No pairing between x and y examples needed!

ClimAlign architecture



- Architecture follows AlignFlow [Grover et al., 2020]
- Normalizing flow: Glow [Kingma & Dhariwal, 2018]

Comparison with supervised benchmarks

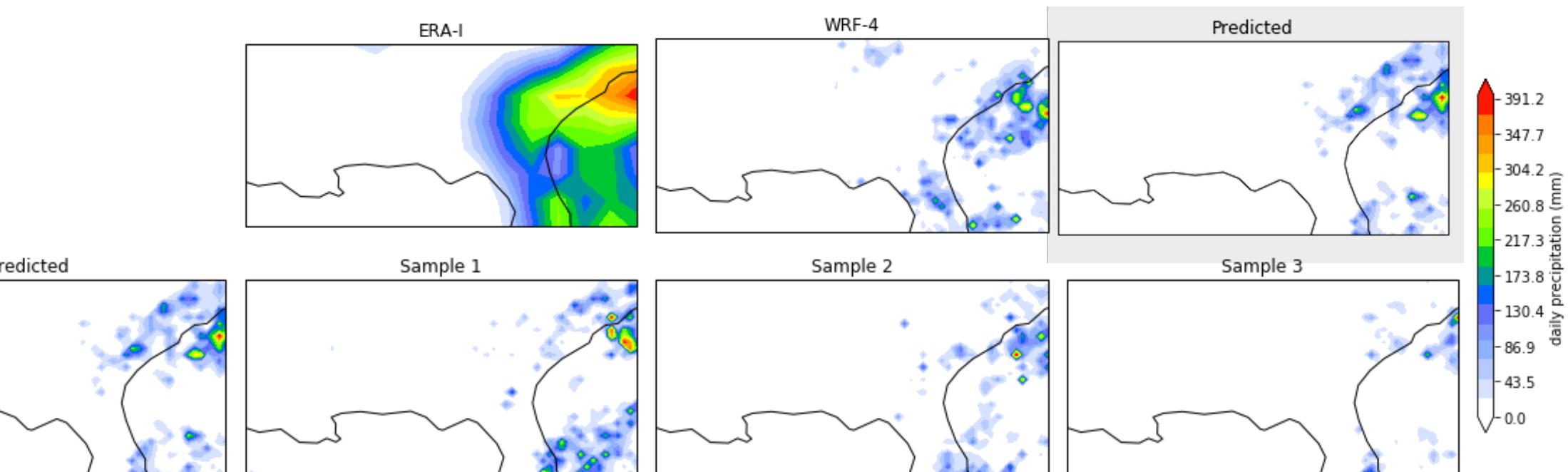
Daily Max Temperature

Region	Method	RMSE	Bias	Corr
SE-US	BCSD	1.51 ± 0.15	-0.02 ± 0.21	0.93 ± 0.05
	BMD-CNN	1.30 ± 0.12	0.03 ± 0.13	0.90 ± 0.05
	ClimAlign (ours)	1.56 ± 0.13	-0.005 ± 0.22	0.87 ± 0.06
P-NW	BCSD	1.54 ± 0.23	0.01 ± 0.10	0.95 ± 0.03
	BMD-CNN	1.25 ± 0.14	-0.06 ± 0.05	0.93 ± 0.02
	ClimAlign (ours)	1.58 ± 0.18	0.03 ± 0.15	0.89 ± 0.04

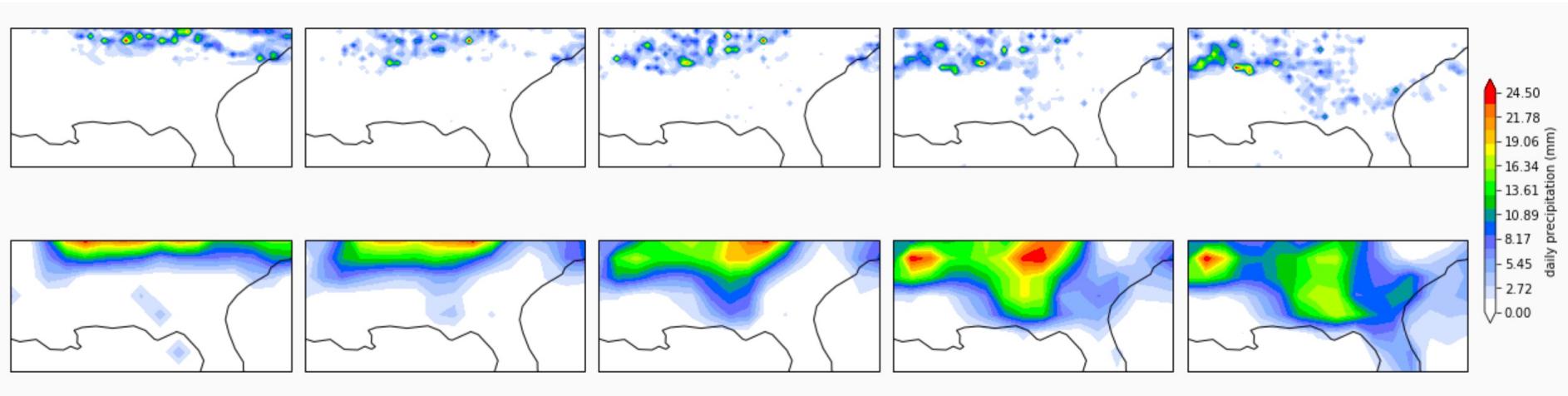
Daily Precipitation

Region	Method	RMSE	Bias	Corr
SE-US	BCSD	27.32 ± 5.0	0.95 ± 1.4	0.39 ± 0.07
	BMD-CNN	14.11 ± 2.18	-0.23 ± 0.47	0.50 ± 0.10
	ClimAlign (ours)	18.40 ± 2.64	0.08 ± 0.86	0.42 ± 0.07
P-NW	BCSD	8.90 ± 2.30	0.41 ± 0.26	0.61 ± 0.06
	BMD-CNN	5.77 ± 0.72	-0.18 ± 0.61	0.70 ± 0.03
	ClimAlign (ours)	7.33 ± 0.69	0.54 ± 0.54	0.67 ± 0.03

Point prediction example



ClimAlign: Unsupervised, generative downscaling



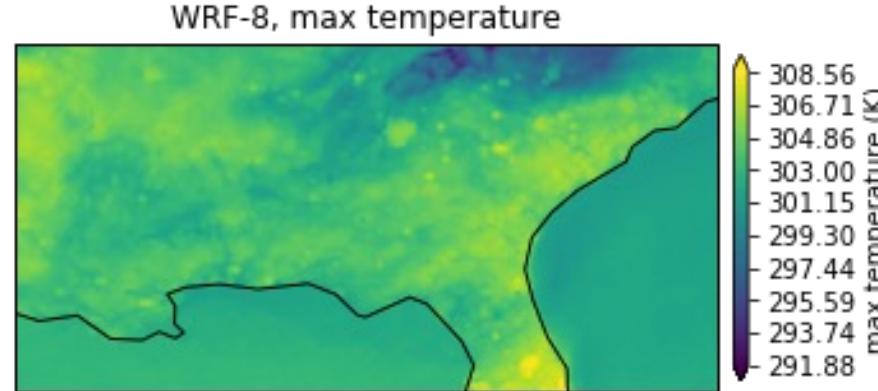
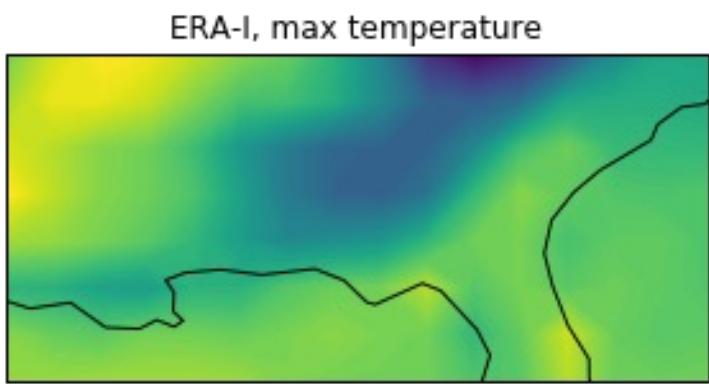
[Groenke et al., CI 2020]

General downscaling technique via domain alignment with normalizing flows
[AlignFlow: Grover et al., AAAI 2020][Glow: Kingma & Dhariwal, NeurIPS 2018]

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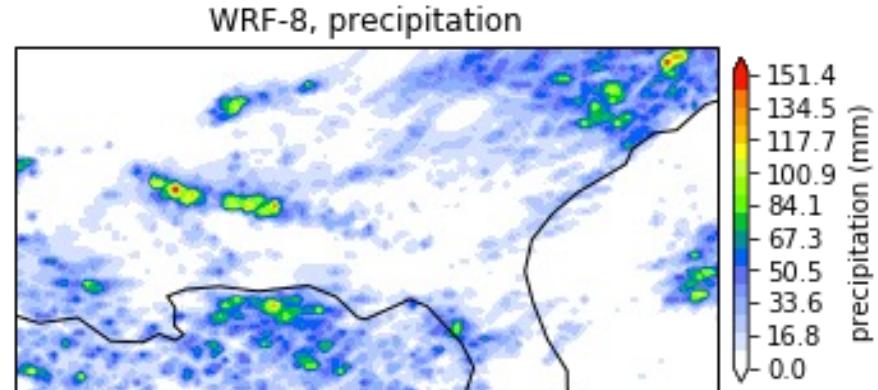
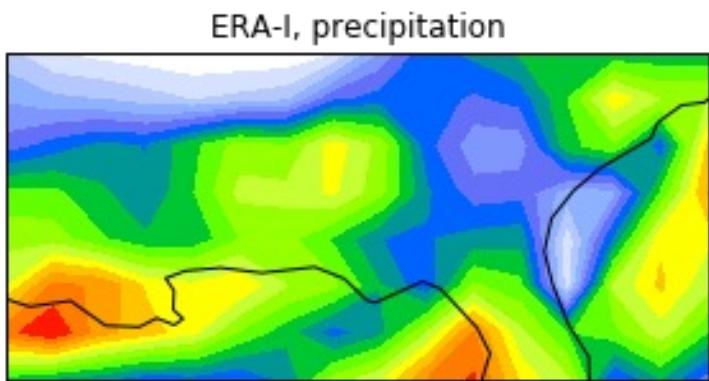
Downscaling: training data

ERA: reanalysis data, 1° resolution; WRF: numerical weather model prediction, $\frac{1}{8}^{\circ}$ resolution



max temperature (K)

308.56
306.71
304.86
303.00
301.15
299.30
297.44
295.59
293.74
291.88



precipitation (mm)

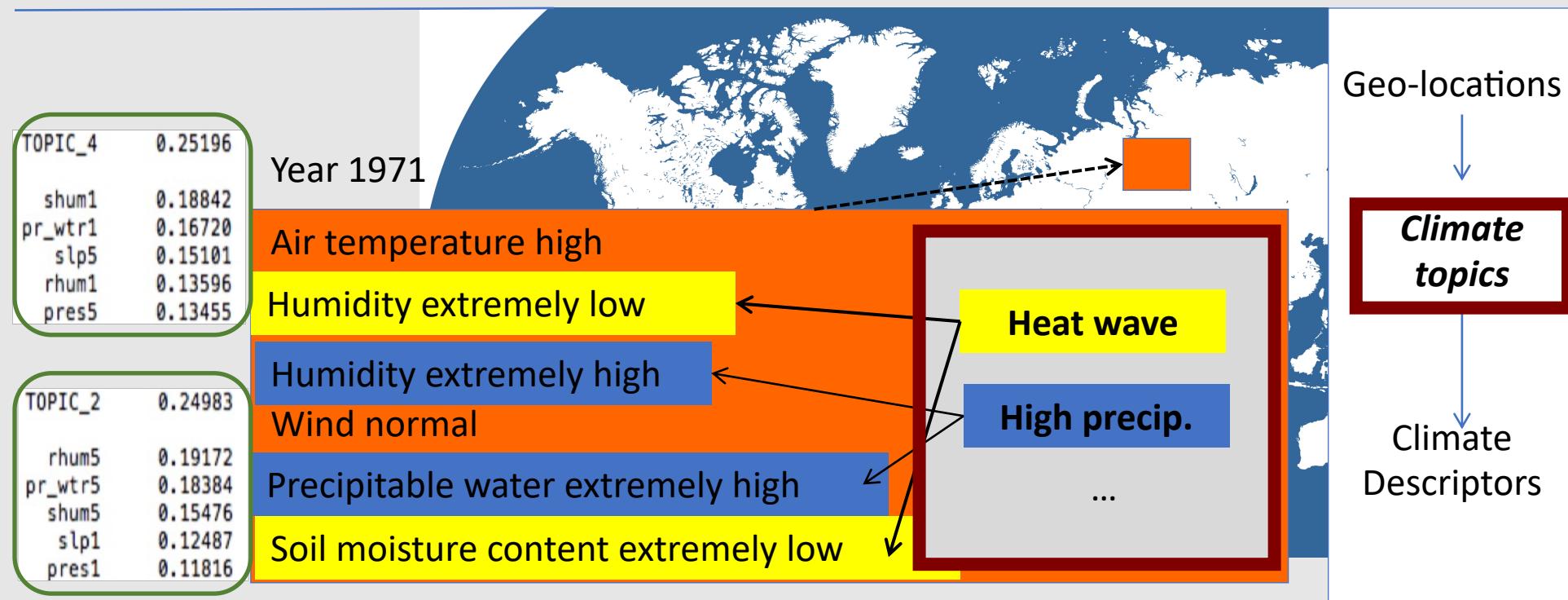
151.4
134.5
117.7
100.9
84.1
67.3
50.5
33.6
16.8
0.0

Unsupervised learning to define/detect multivariate extremes

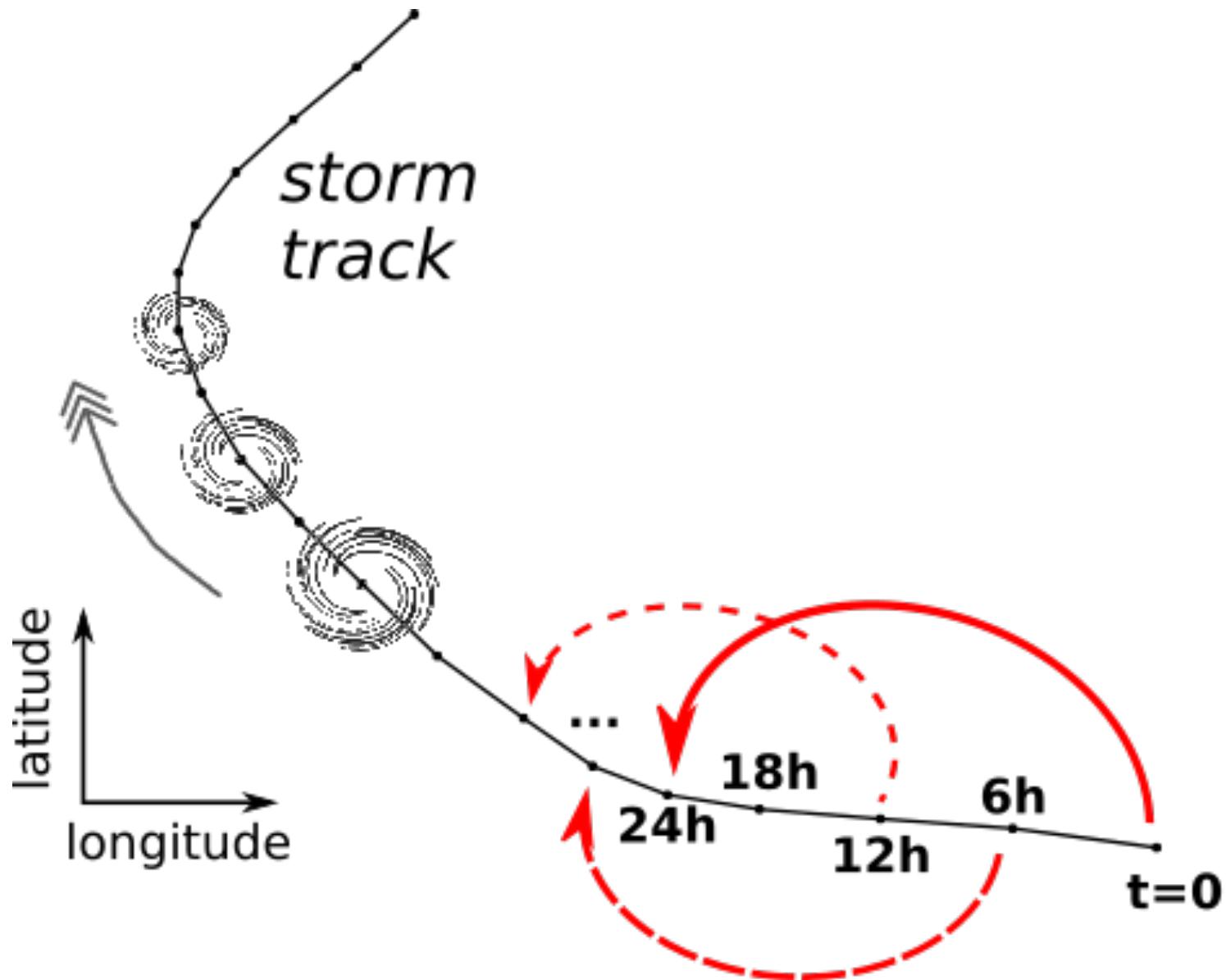
[Tang & M, Climate Informatics 2014; IEEE CISE 2015]

Extend probabilistic topic modeling (Latent Dirichlet Allocation [Blei et al., 2001]) from NLP

- **Multiple variables** (complex, multivariate extreme events)
- Ability to detect **multiple types** of events
- Multiple degrees of severity
- Uses all data, not just extreme values



Forecasting task: 24h spatial displacement



Related work

- Define a region (hurricane basin)
- Estimate future location as (x,y) coordinates
- Training set: storms from the same basin

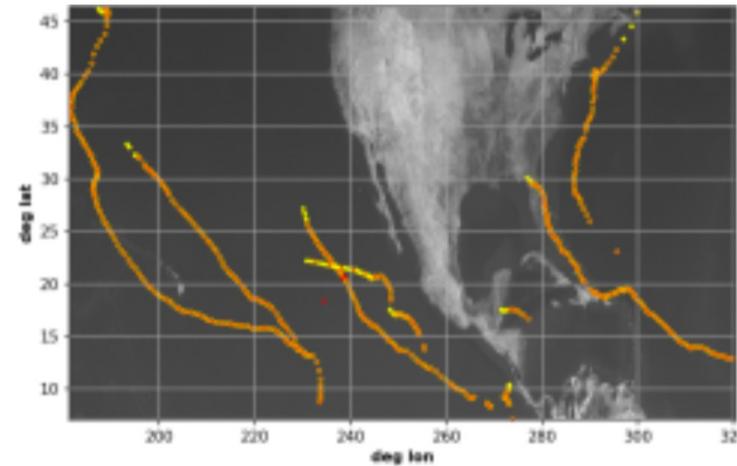
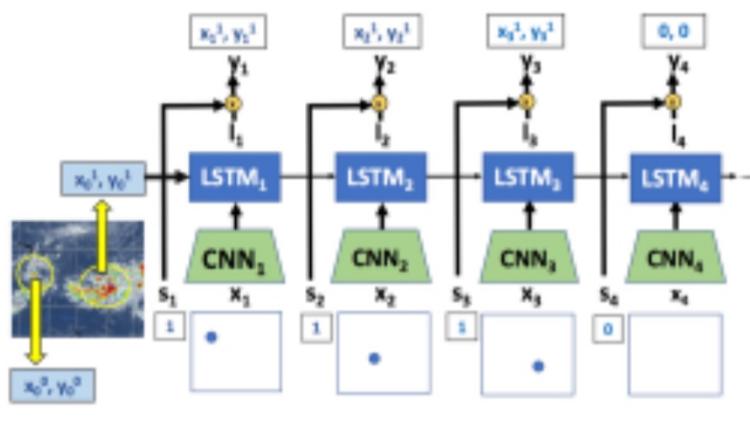
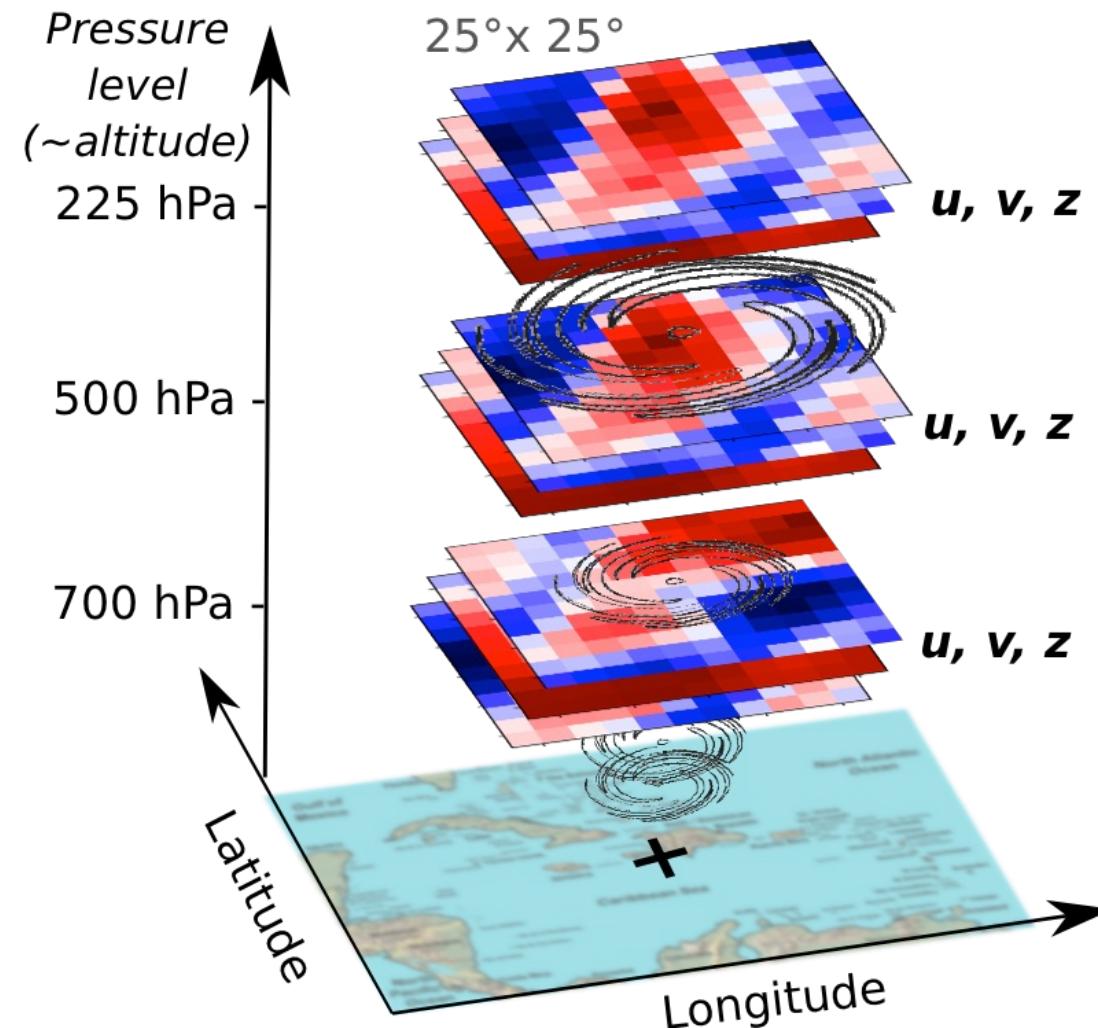


Figure: Mudigonda et. al, DLPS Workshop at NIPS 2017

Our approach: moving frame-of-reference

- Estimate future **displacement** as $\vec{u} = (dx, dy)$
- Centered reanalysis data (center = current storm location)

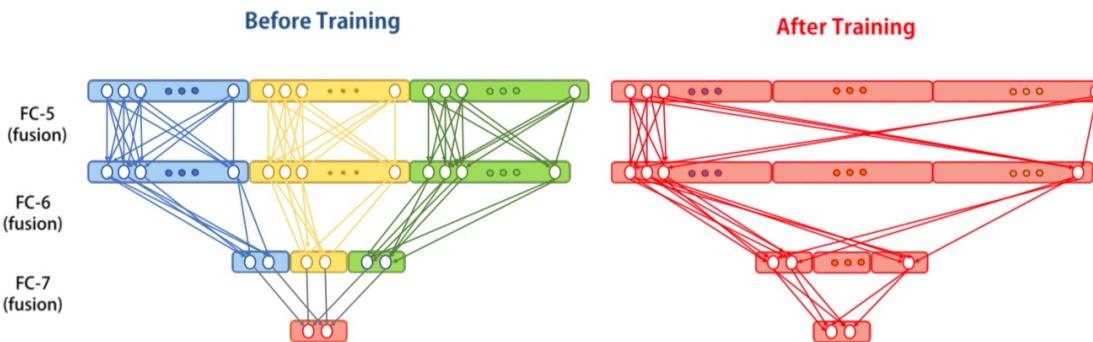


Data types

- *Wind and pressure fields*: at 3 pressure levels (700 hPa, 500 hPa, and 225 hPa); at times t and $t - 6h$ (**2D+t**)
- *Past displacements*: \vec{u}_{t-6h} and \vec{u}_{t-12h} (**0D+t**)
- *Other hand-crafted features*: (**0D**):
 - current latitude / longitude
 - windspeed
 - Jday predictor(Gaussian function of "Julian day of storm init - peak day of the hurricane season")
 - current distance to land

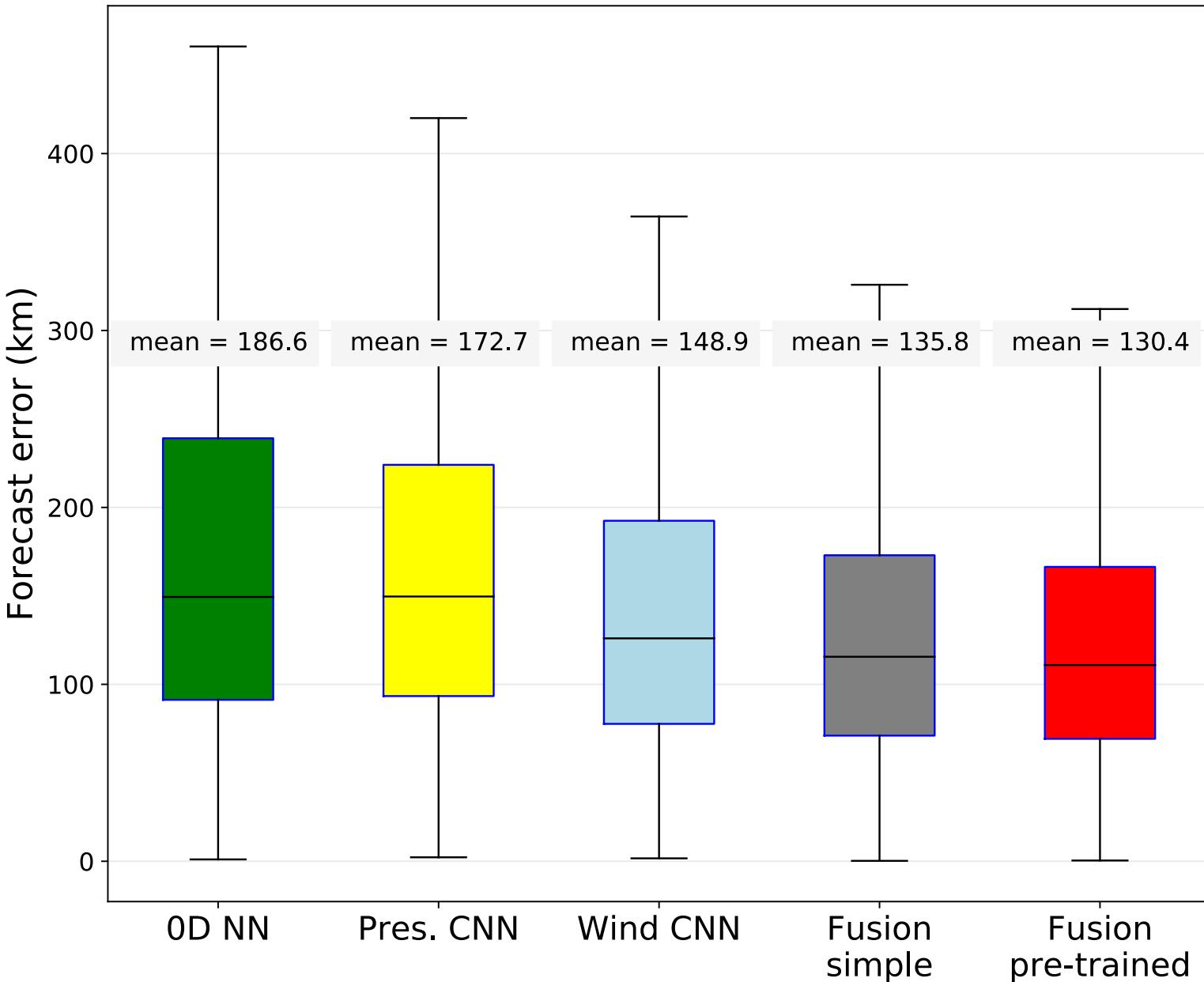
Training the fusion network

- Stage I: Train separate networks
- Stage II: Train the fusion network
 - Zoom in fusion layers:



- Add connections between different streams in fusion layers
- Re-train the whole network

Performance of network components



State of the art

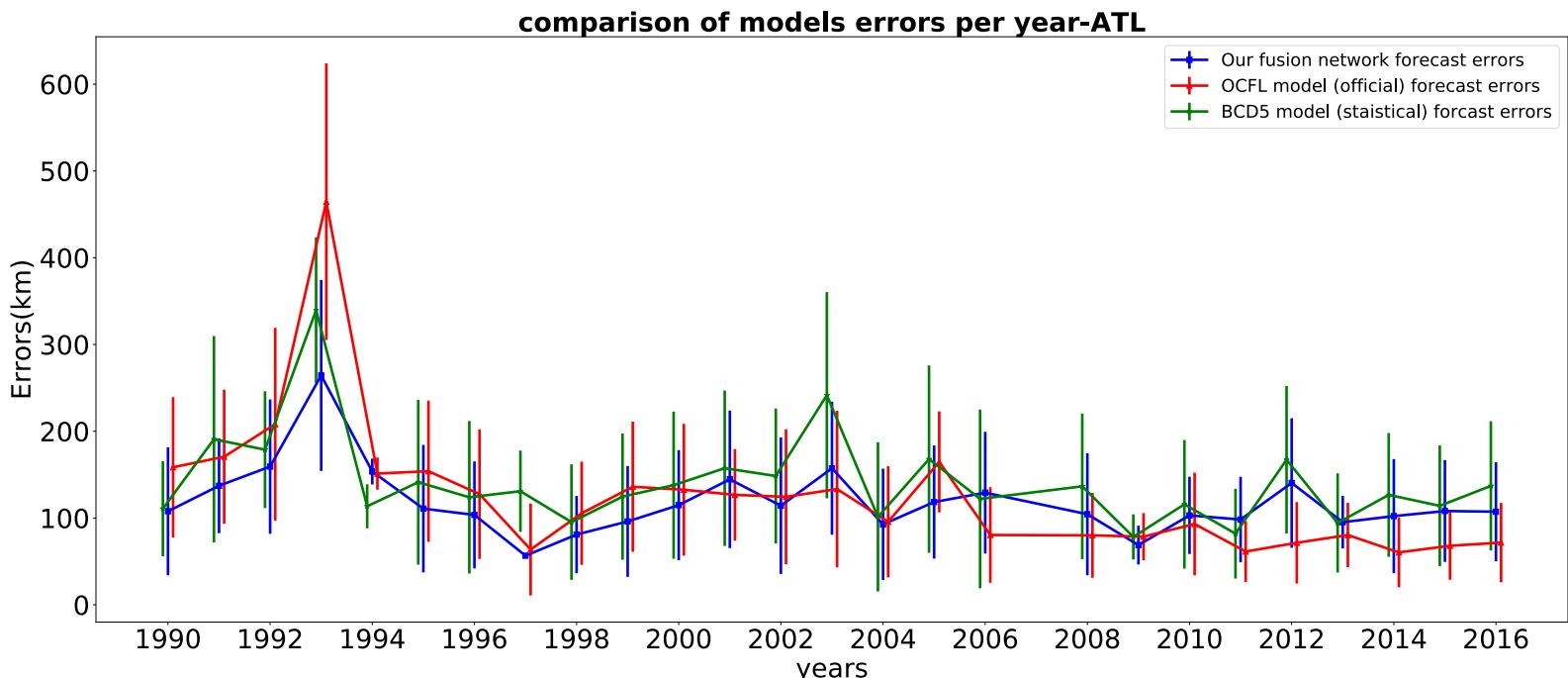
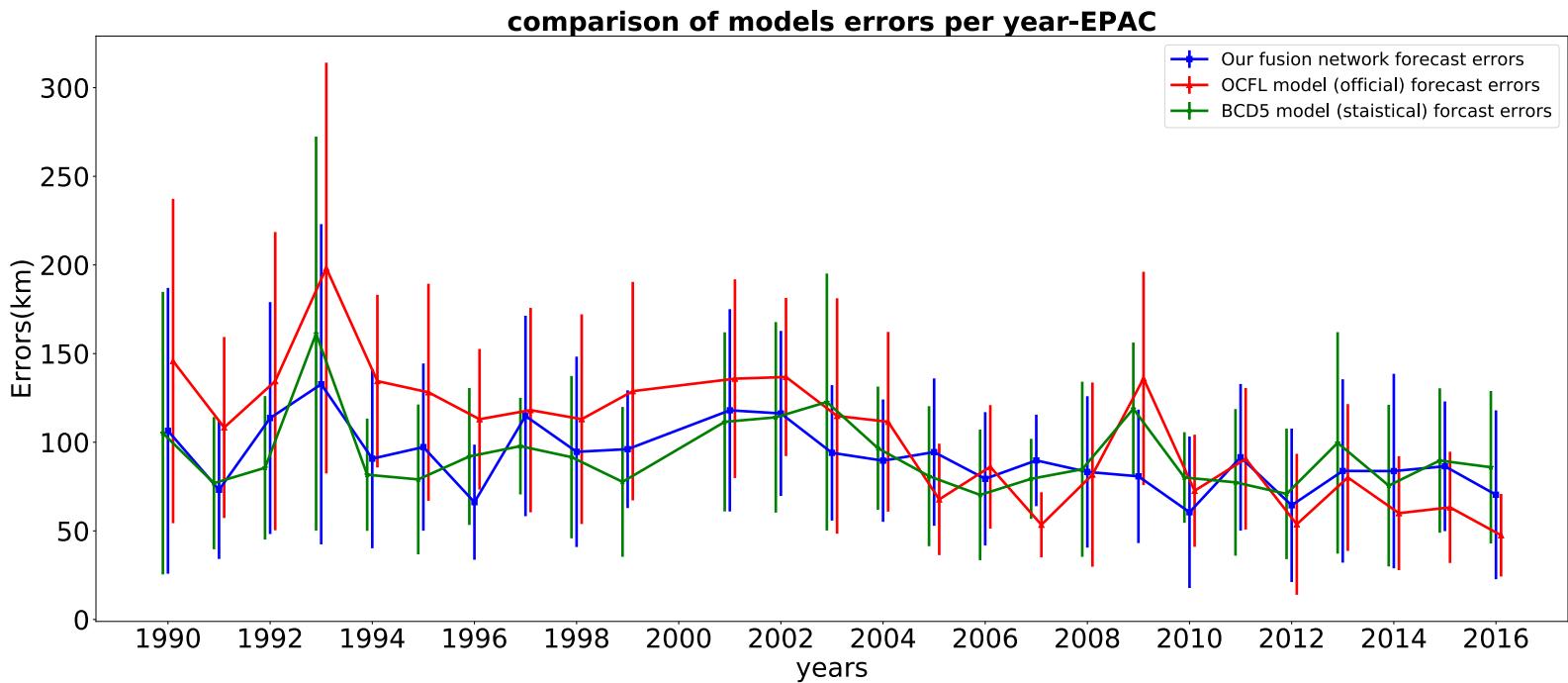
- **BCD5** : statistical model, often used to benchmark other storm track forecasting methods
- **OFCL** : National Hurricane Center official forecast (consensus of dynamical models), BUT evolving over years

Model	Atlantic errors (km)		East Pacific errors (km)	
	mean error	std	mean error	std
BCD5	125	90	112	78
Fusion	112	71	88	52

Table: Mean and standard deviation 24h-forecast errors for the Atlantic and Pacific basins on part of the test set (total = 4349 time steps)

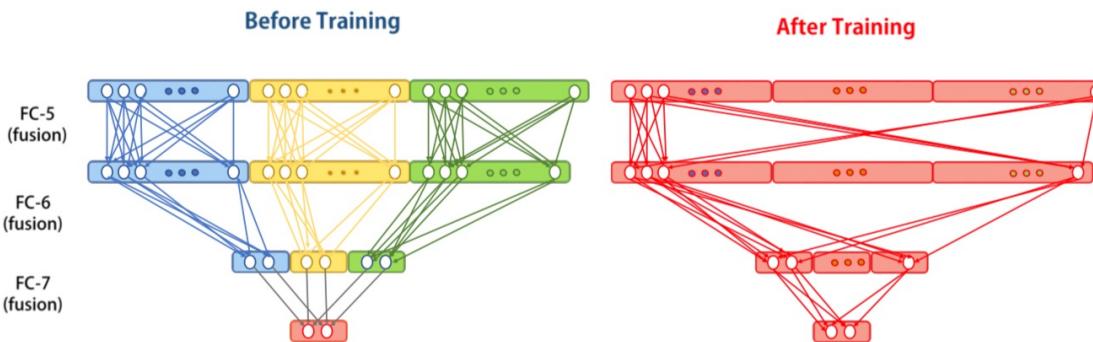
- Mean error across all basins, time steps from hurricanes only: **103.9 km**
- [Climate Informatics '18]: 6h prediction error, same evaluation: **28.5 km**

Cor



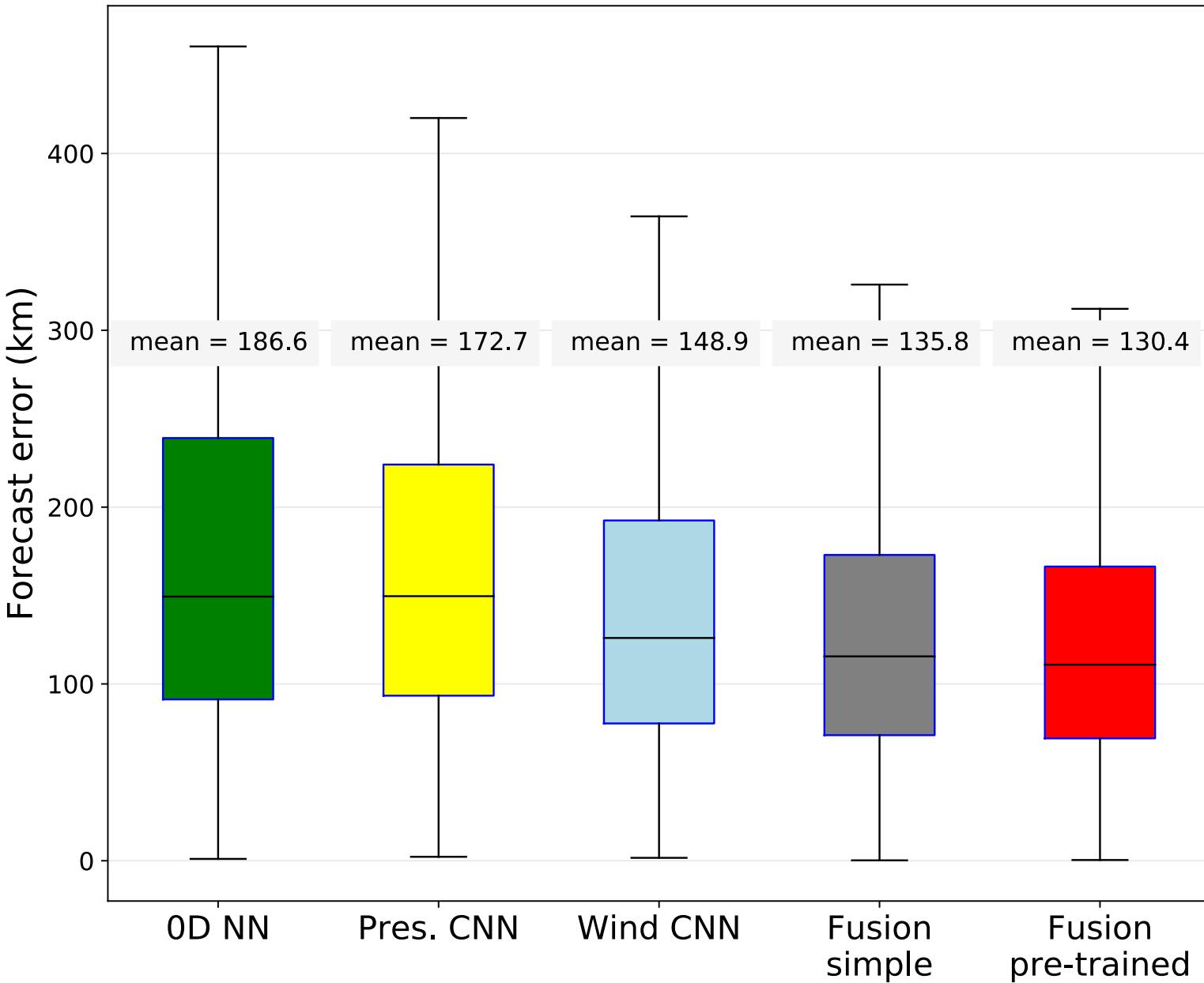
Training the fusion network

- Stage I: Train separate networks
- Stage II: Train the fusion network
 - Zoom in fusion layers:



- Add connections between different streams in fusion layers
- Re-train the whole network

Performance of network components



State of the art

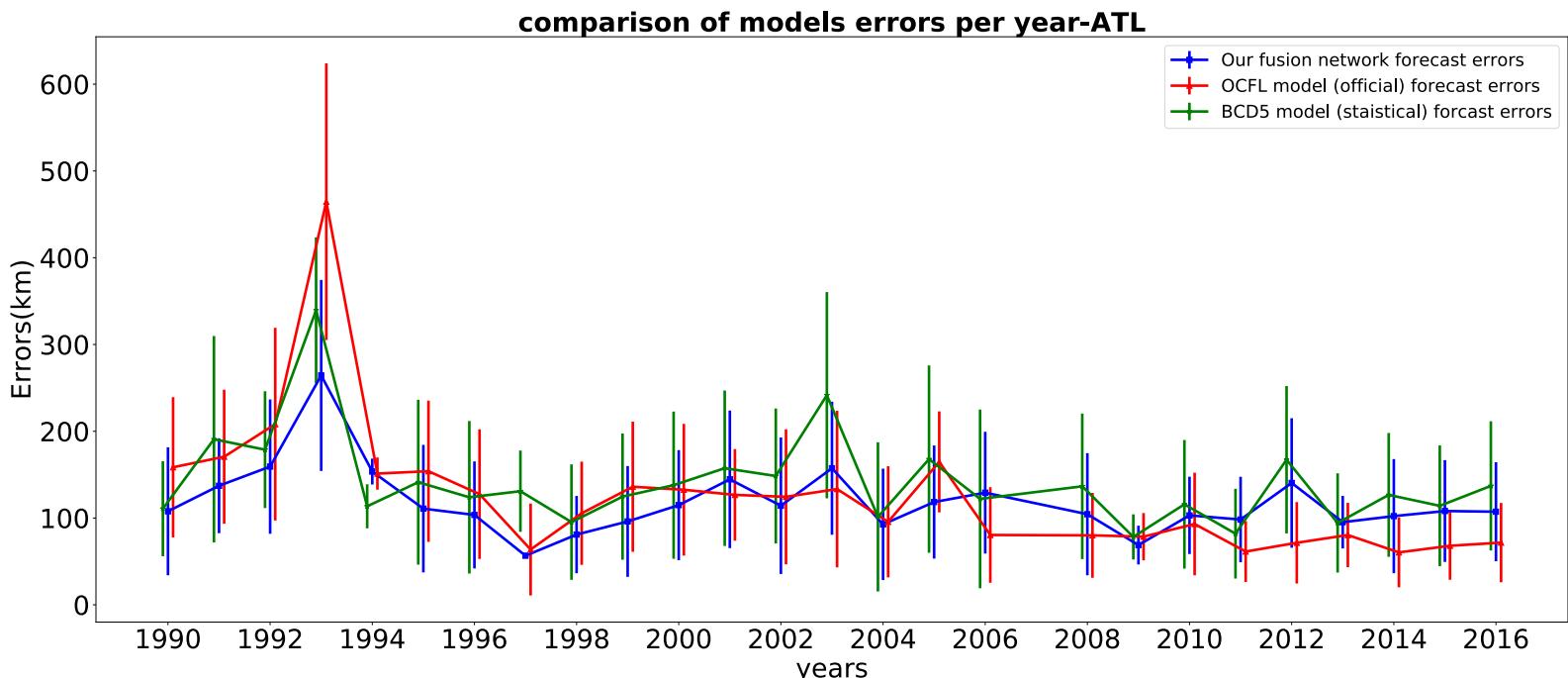
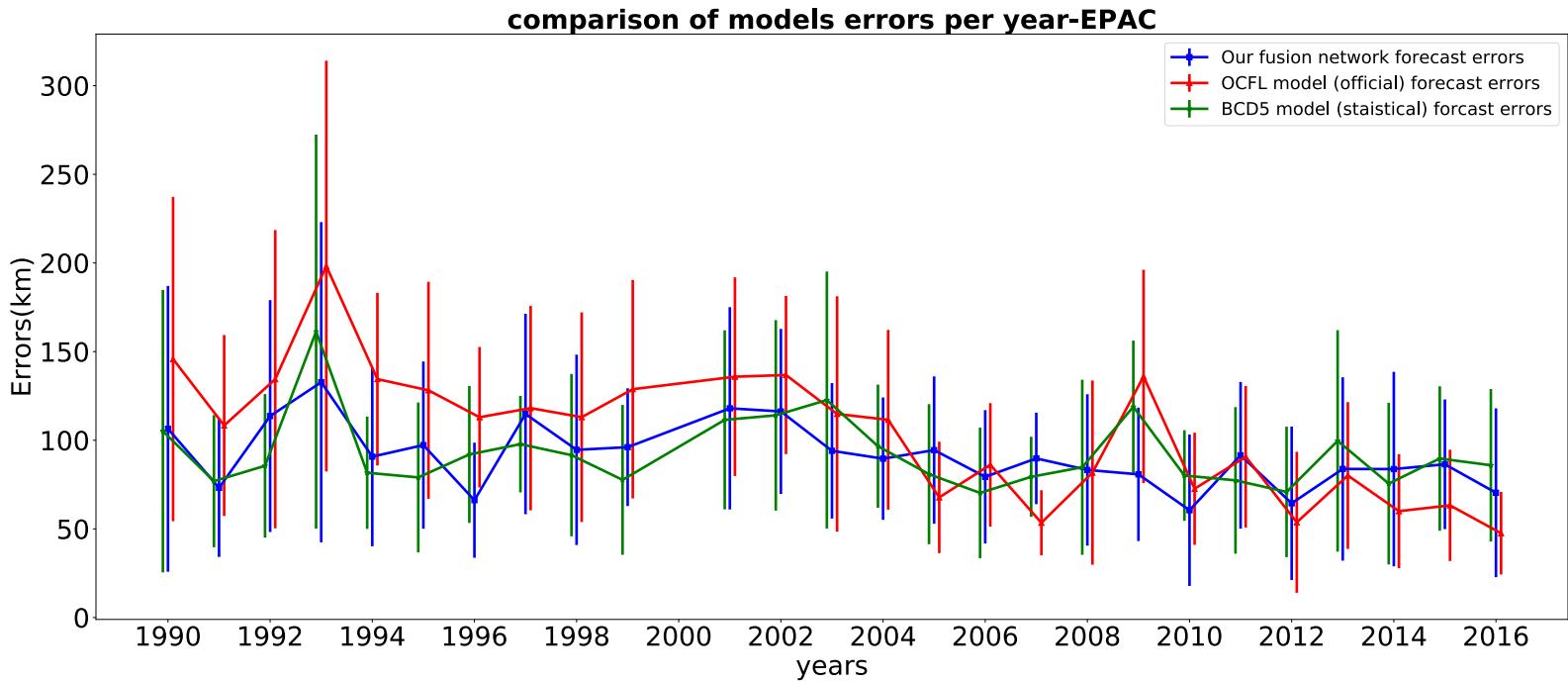
- **BCD5** : statistical model, often used to benchmark other storm track forecasting methods
- **OFCL** : National Hurricane Center official forecast (consensus of dynamical models), BUT evolving over years

Model	Atlantic errors (km)		East Pacific errors (km)	
	mean error	std	mean error	std
BCD5	125	90	112	78
Fusion	112	71	88	52

Table: Mean and standard deviation 24h-forecast errors for the Atlantic and Pacific basins on part of the test set (total = 4349 time steps)

- Mean error across all basins, time steps from hurricanes only: **103.9 km**
- [Climate Informatics '18]: 6h prediction error, same evaluation: **28.5 km**

Cor



Avalanche Detection



Img src : <https://www.nytimes.com/2017/01/19/world/europe/italy-avalanche.html>

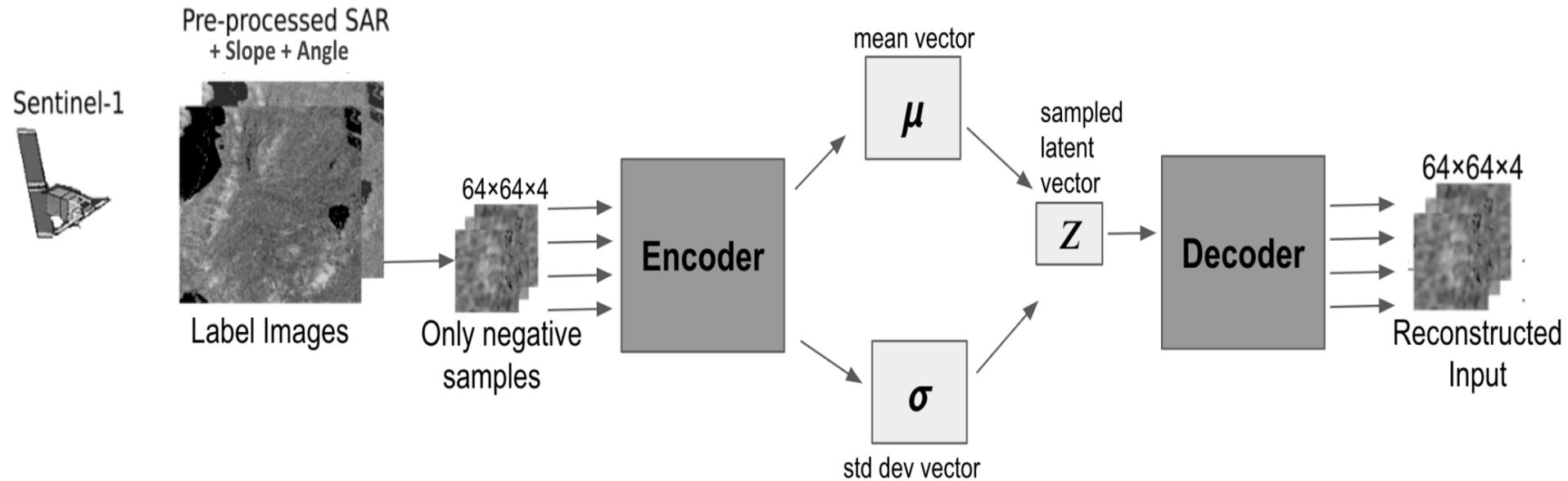
Challenges for Machine Learning

- Severe class imbalance
 - Avalanches are rare events
- Ground-truth labeled data difficult to obtain
 - Terrain accessibility
 - Weather conditions
 - Danger of avalanches

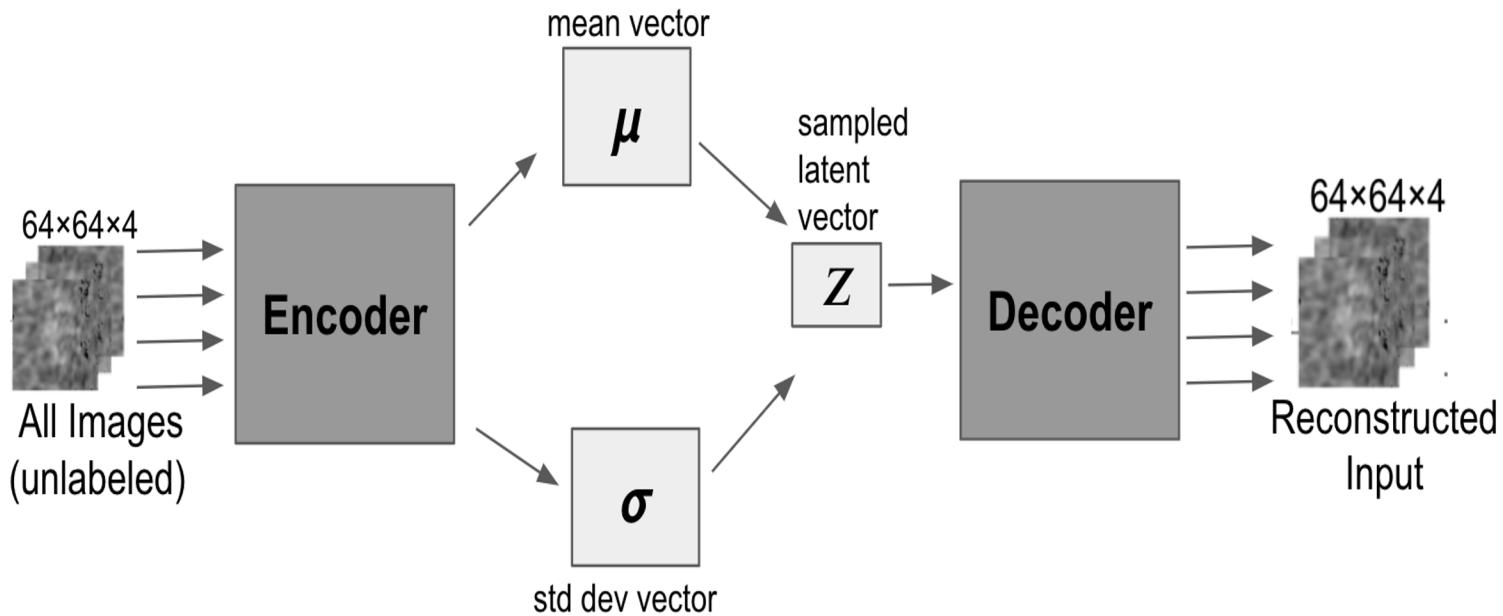
Our Approach

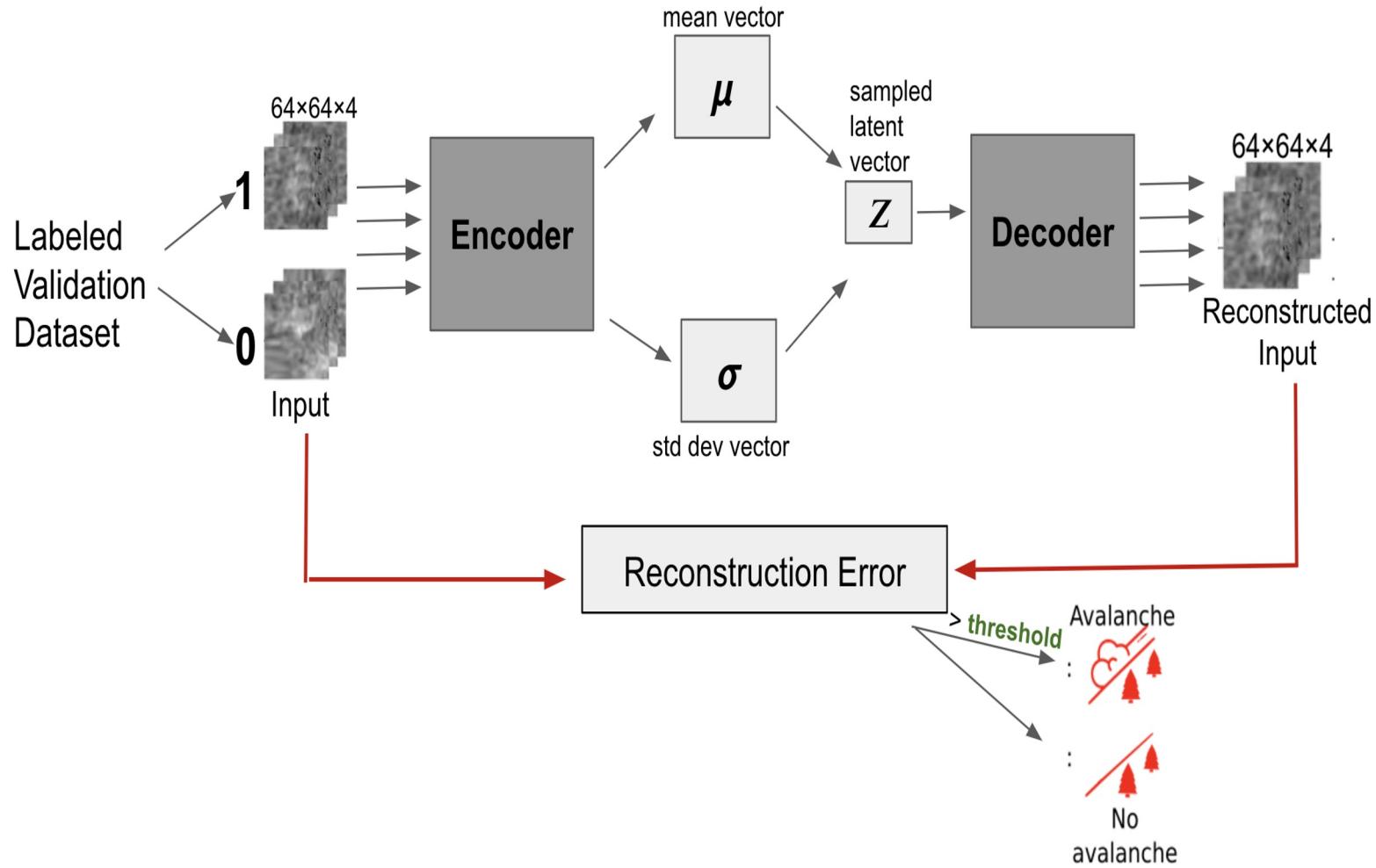
- ① Treat an avalanche as a rare event, or an anomaly
 - ② Train a variational autoencoder (VAE) on the negative examples
 - ③ Threshold the VAE's reconstruction error to classify a new image
- When labeled data is scarce, the VAE can instead be trained **without** supervision!

VAE trained on negative examples



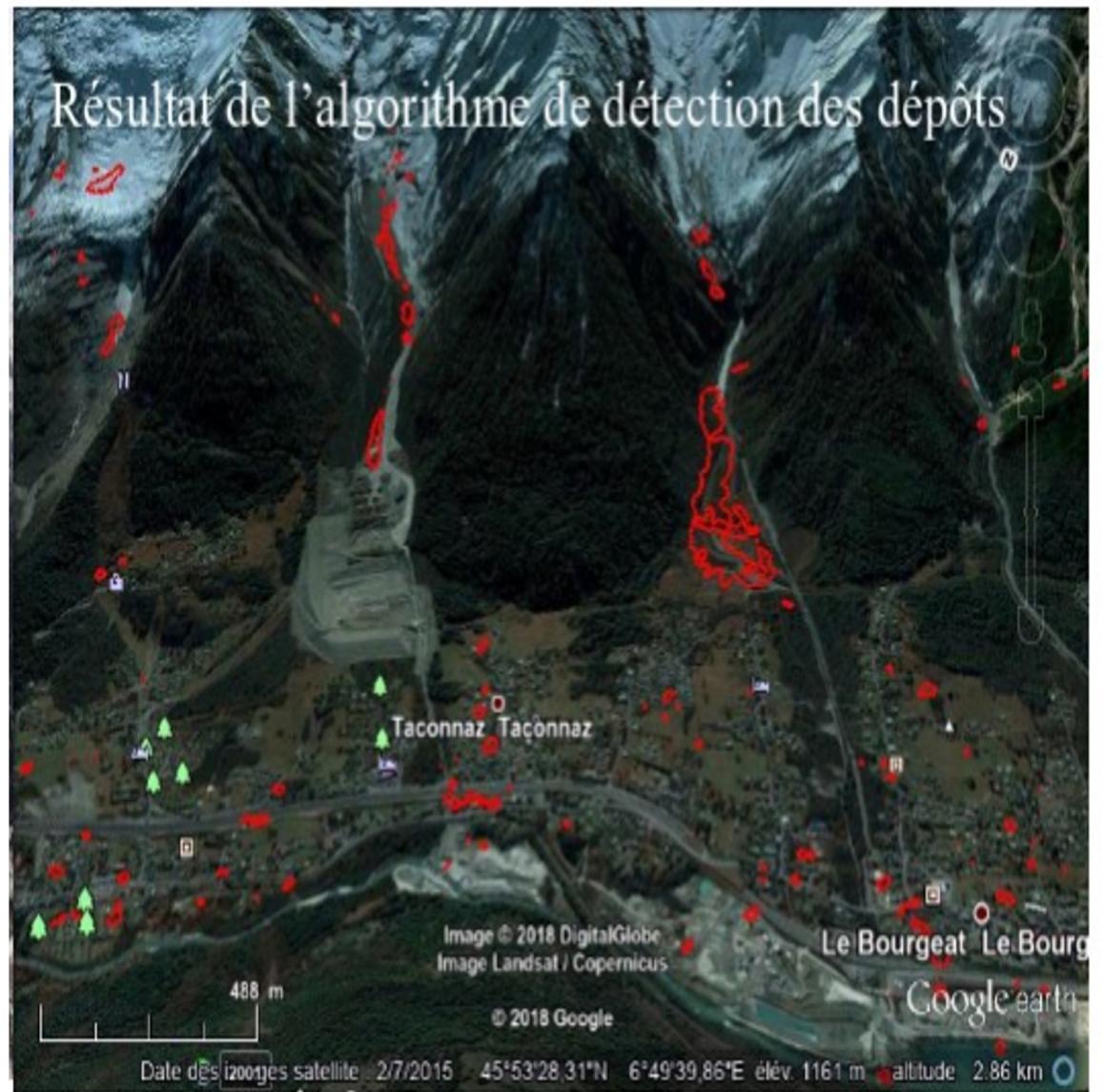
VAE trained on ALL examples





Tuning the threshold for Anomaly Detection

Baseline method: Thresholding



[Karbou et al., International Snow Science Workshop 2018 & EGU 2018]

Evaluation

One of the most susceptible mountain chains (out of the 18 in “All Alps”)

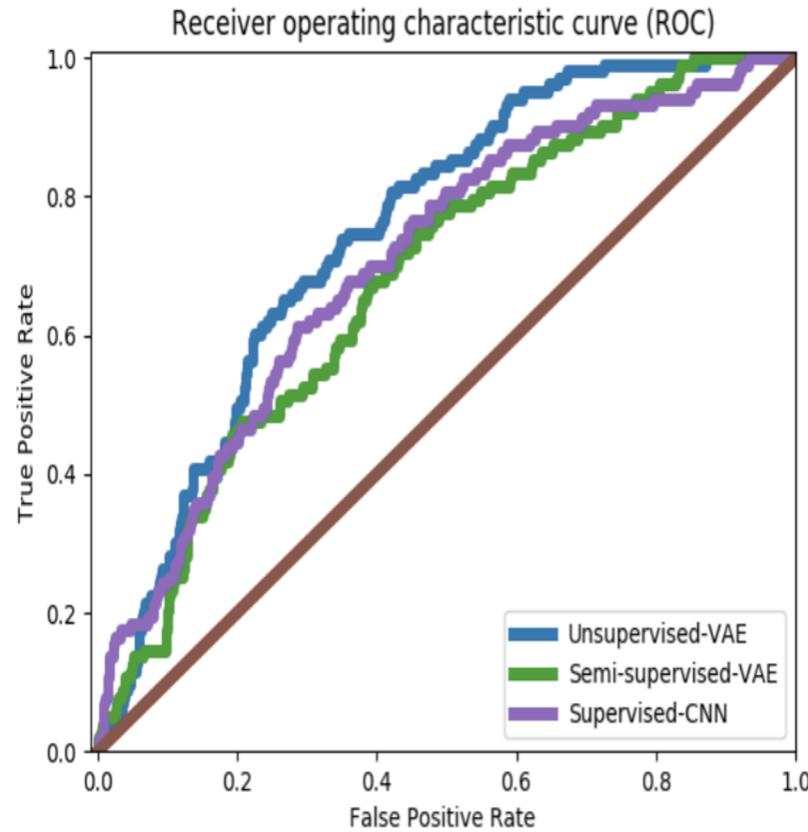


	All Alps		Haute Maurienne	
	Balanced Accuracy	F1-score	Balanced Accuracy	F1-score
Baseline	0.58	0.05	0.58	0.12
Supervised - CNN	0.53	0.10	0.53	0.12
Semi-supervised - VAE	0.59	0.11	0.6	0.23
Unsupervised - VAE	0.69	0.14	0.68	0.26

- Held-out test set: 6,498 labeled examples
- Baseline method from avalanche-detection literature: Thresholding [Karbou et al., ISSW 2018]
- Supervised-learning benchmark method: Convolutional Neural Network (CNN) trained on artificially balanced dataset [Sinha et al., Climate Informatics 2019]

Evaluation

ROC Curves for Haute Maurienne region



Method	AUC ROC
Supervised - CNN	70.7
Semi-supervised - VAE	68.3
Unsupervised - VAE	75

Outlook

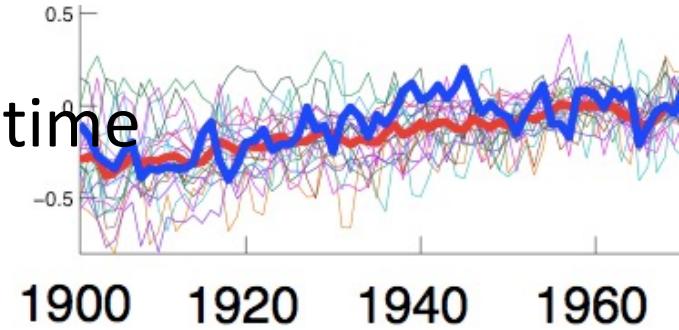
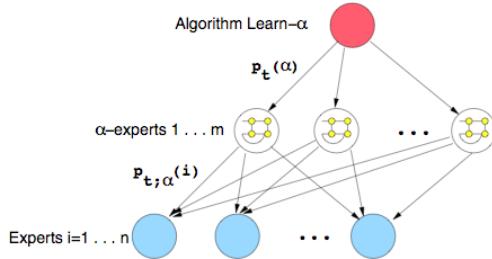
- Provided a semi-supervised approach to detecting rare events when labeled data is limited
- Can be viewed as a form of virtual sensor
- Next step: forecasting

Learning from spatiotemporal data

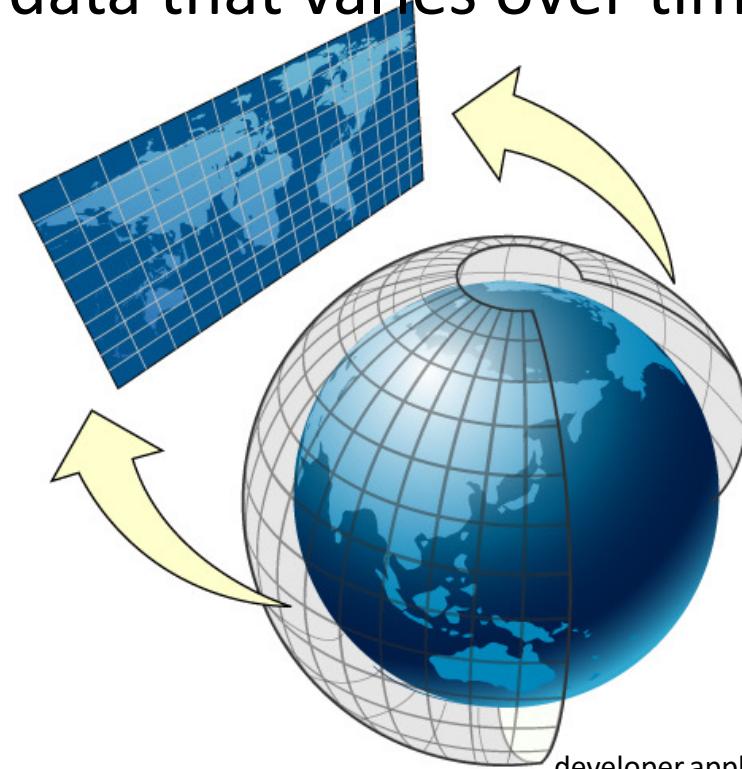
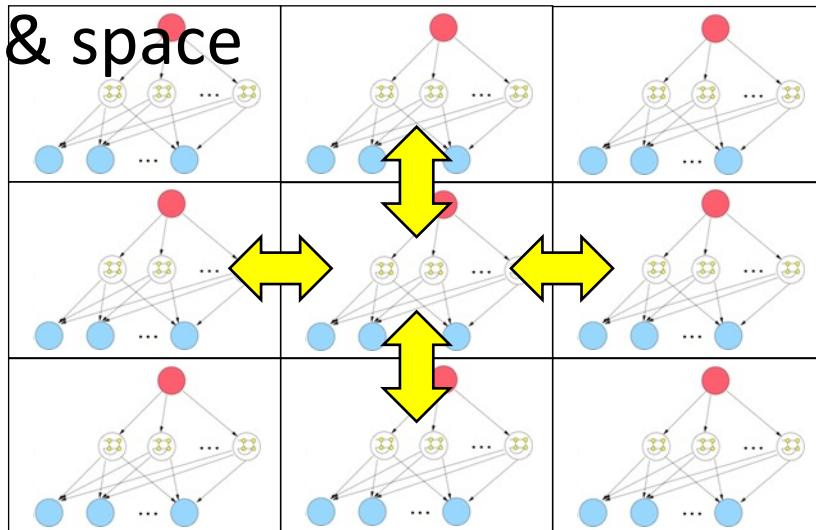
- Learning from non-stationary time series
 - Simultaneously learn the level of non-stationarity
 - Exploit local temporal structure via multi-task learning
- Learning from non-stationary spatiotemporal data
 - Exploit local spatial structure
 - Distributed online learning
 - Hidden Markov random field

Roadmap

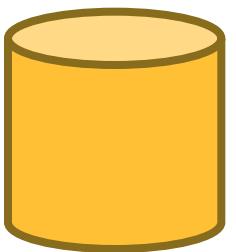
- Learning from data that varies over time



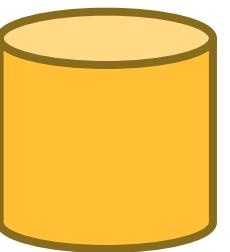
- Learning from spatiotemporal data that varies over time



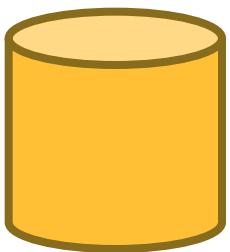
Average prediction



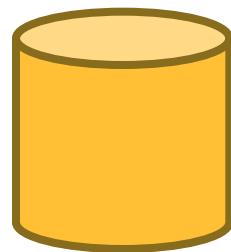
Model A



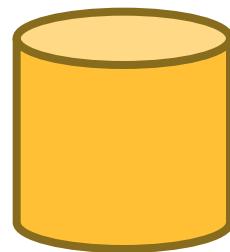
Model B



Model C



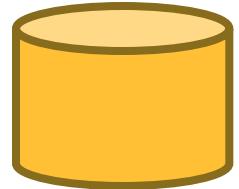
Model D



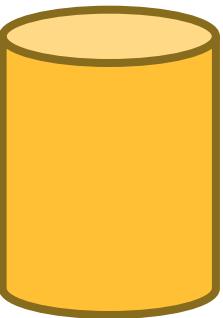
Model E



Adaptive, weighted average prediction



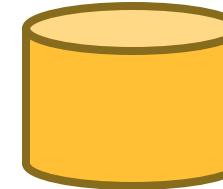
Model A



Model B



Model C



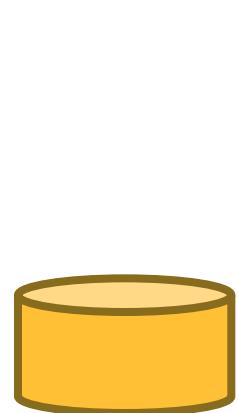
Model D



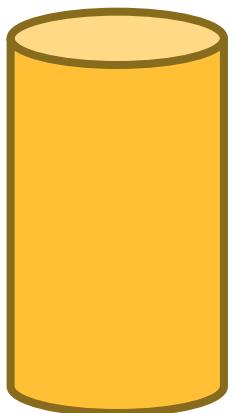
Model E



Adaptive, weighted average prediction



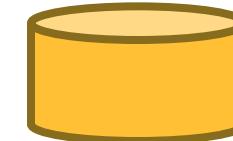
Model A



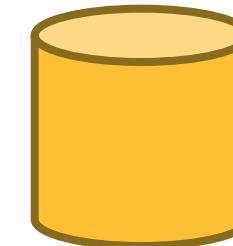
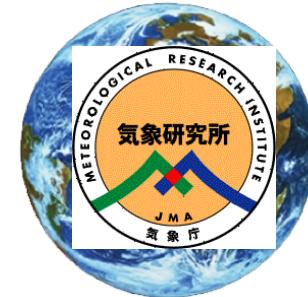
Model B



Model C



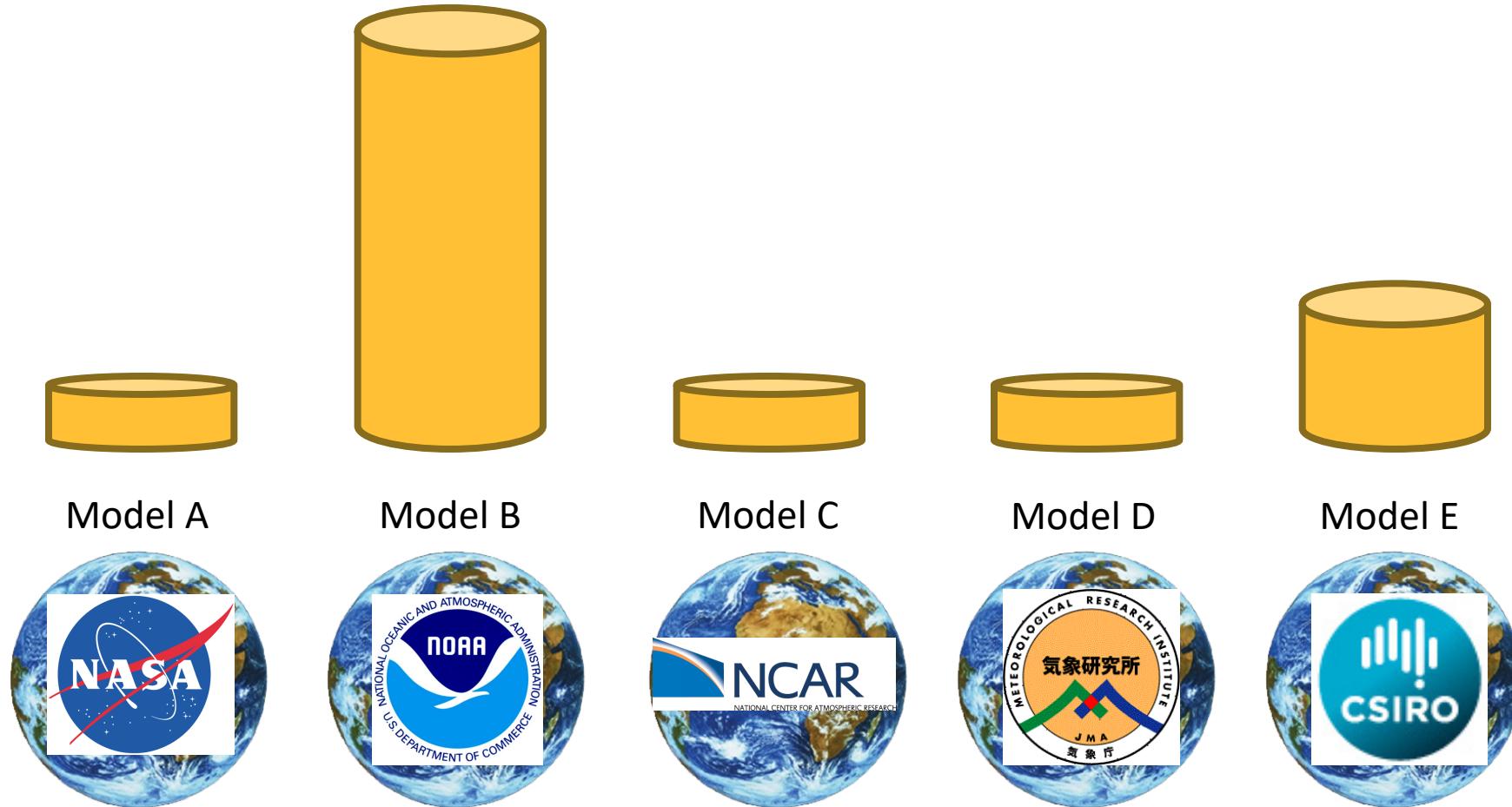
Model D



Model E



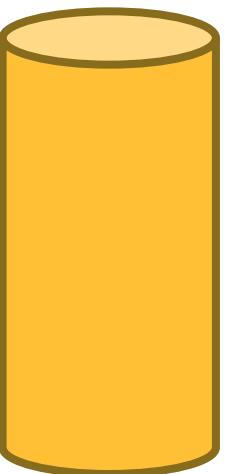
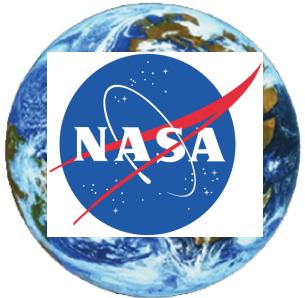
Adaptive, weighted average prediction



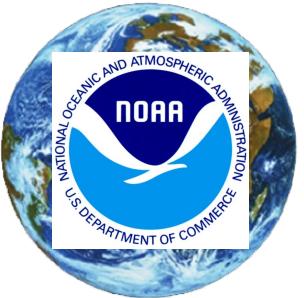
Adaptive, weighted average prediction



Model A



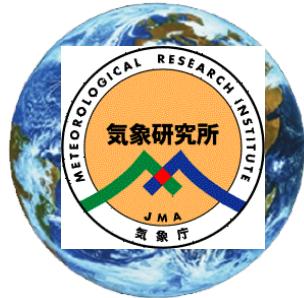
Model B



Model C



Model D



Model E

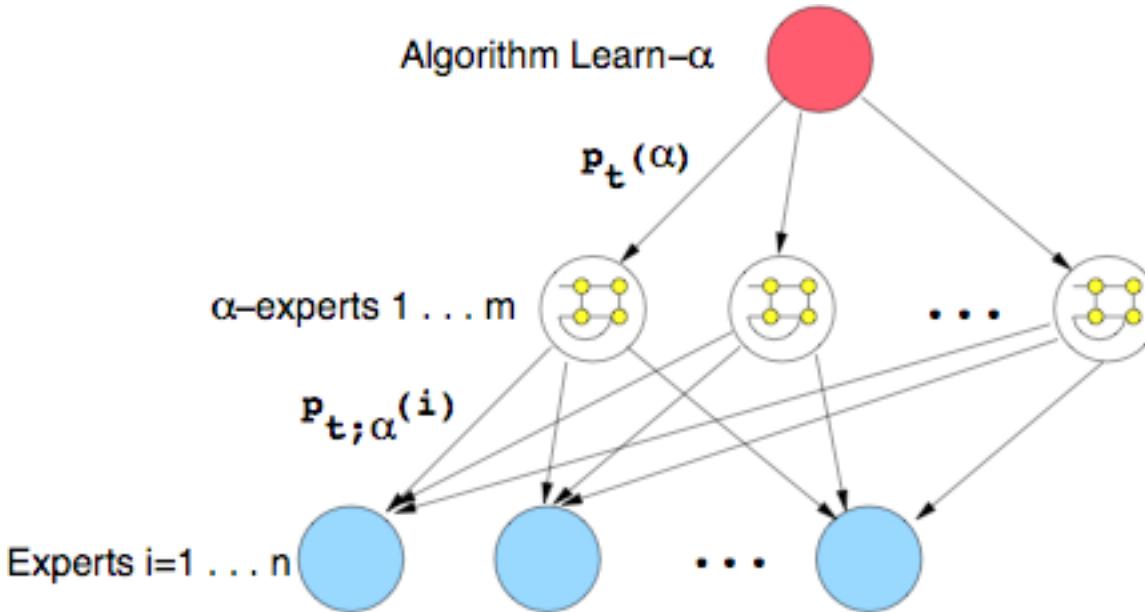


Tradeoff: explore vs. exploit

Tradeoff: Quickly finding **current** best predicting model vs. being ready to quickly **switch** to other models.

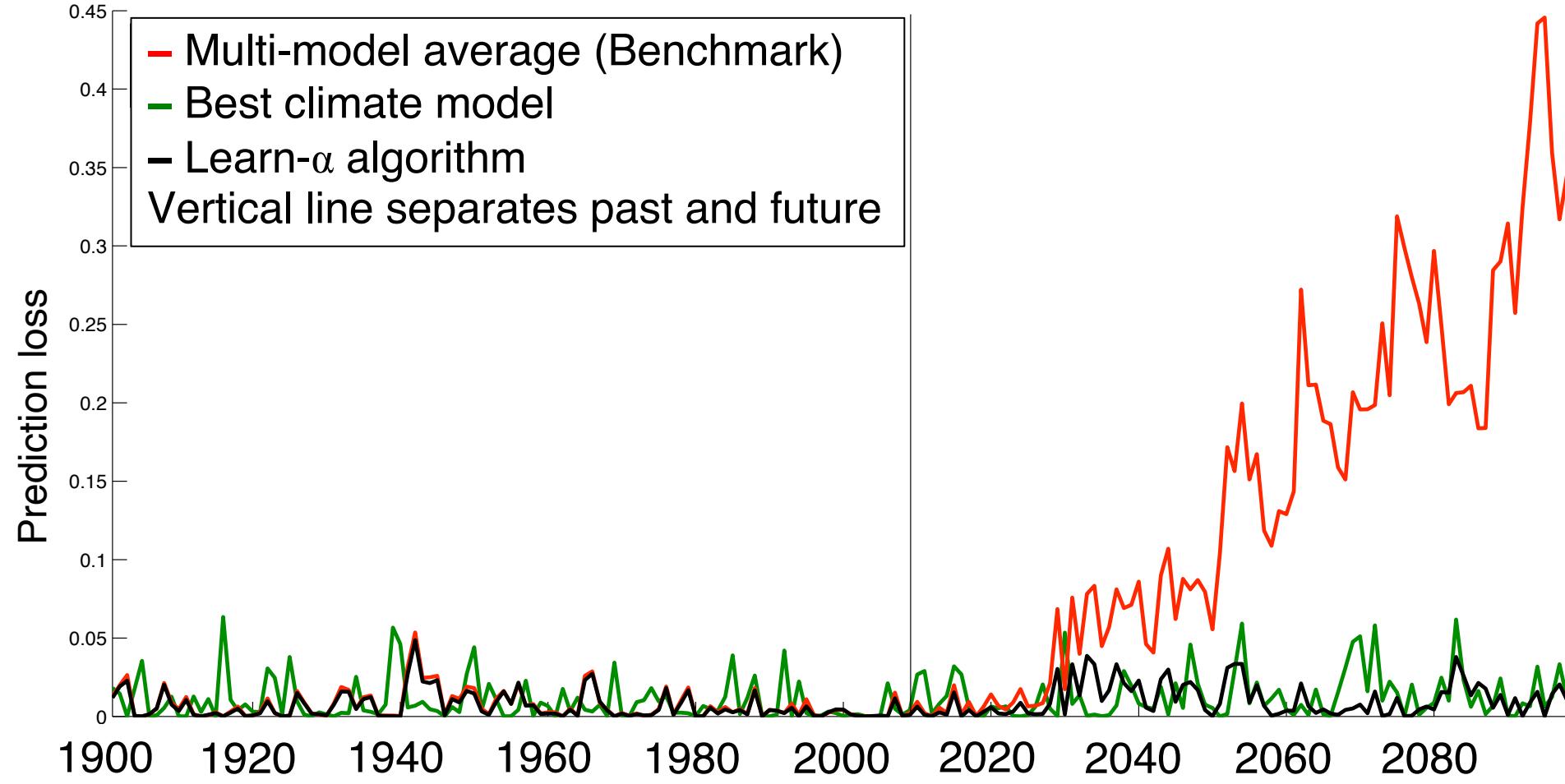
Tradeoff hinges on how often the identity of the best model **switches**.

Online learning: time-varying data



Learn- α Algorithm [Monteleoni & Jaakkola, NeurIPS 2003]:

- **Learns the switching-rate:** level of non-stationarity: α
- Tracks a set of online learning algorithms, each with a different α value
- Each algorithm maintains weights over experts (e.g. climate models)



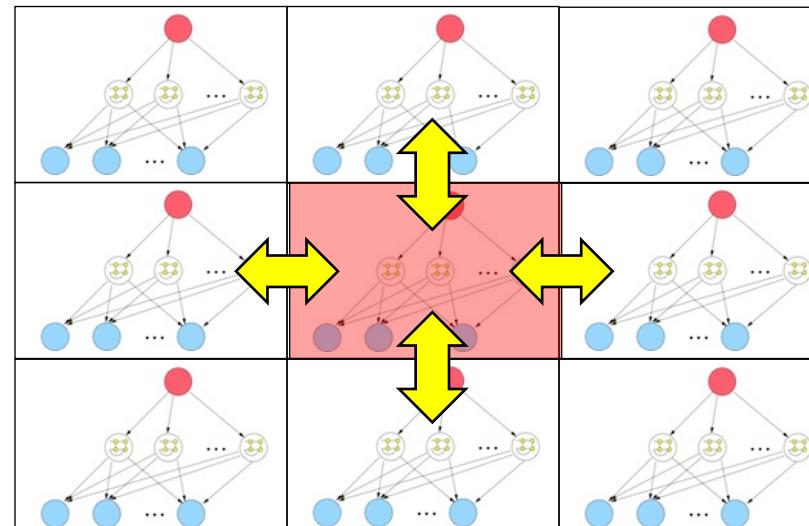
Learning curves

[Monteleoni, Schmidt, Saroha, & Asplund, NASA CIDU 2010; SAM 2011]

Online learning: spatiotemporal data

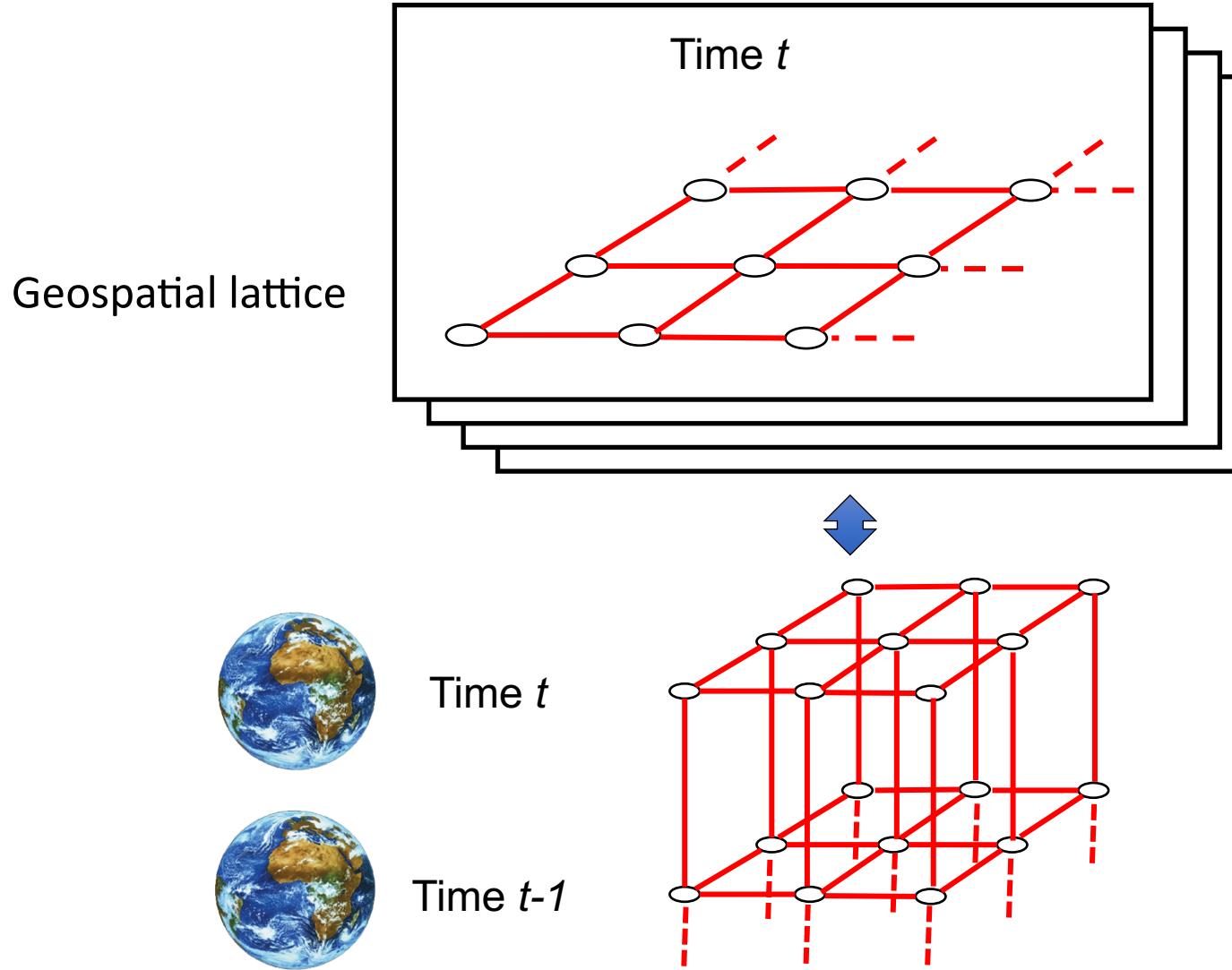
[McQuade & Monteleoni, AAAI 2012]

- Climate predictions are made at **higher geospatial resolutions**
- Run Learn- α (variant) on multiple sub-regions partitioning globe
- Distribution over climate models varies **over both time and space**
- Model neighborhood influences among geospatial regions

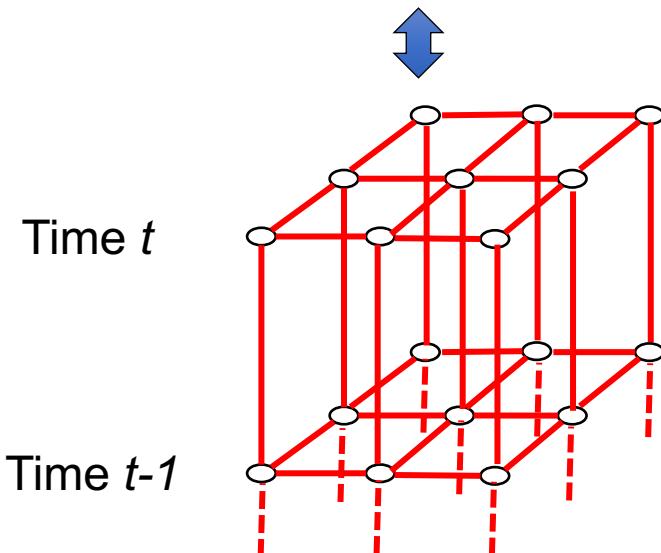
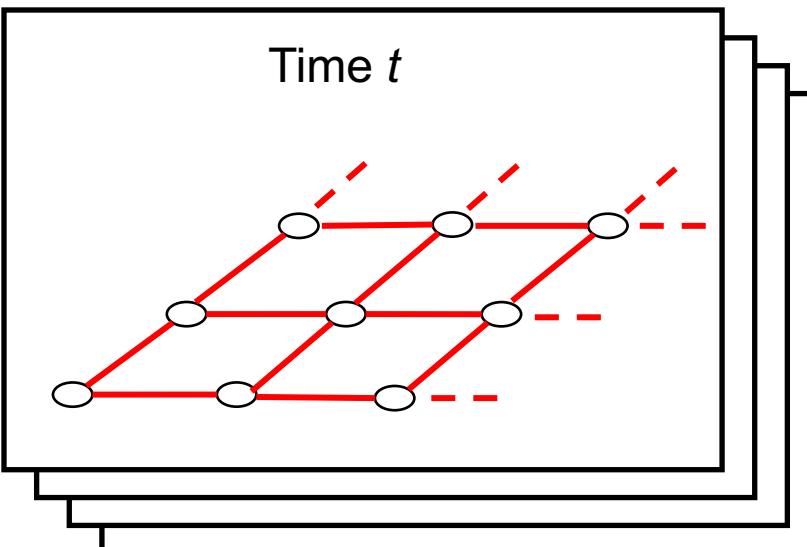


Markov Random Field-based approach

[McQuade & Monteleoni, book chapter, 2017]



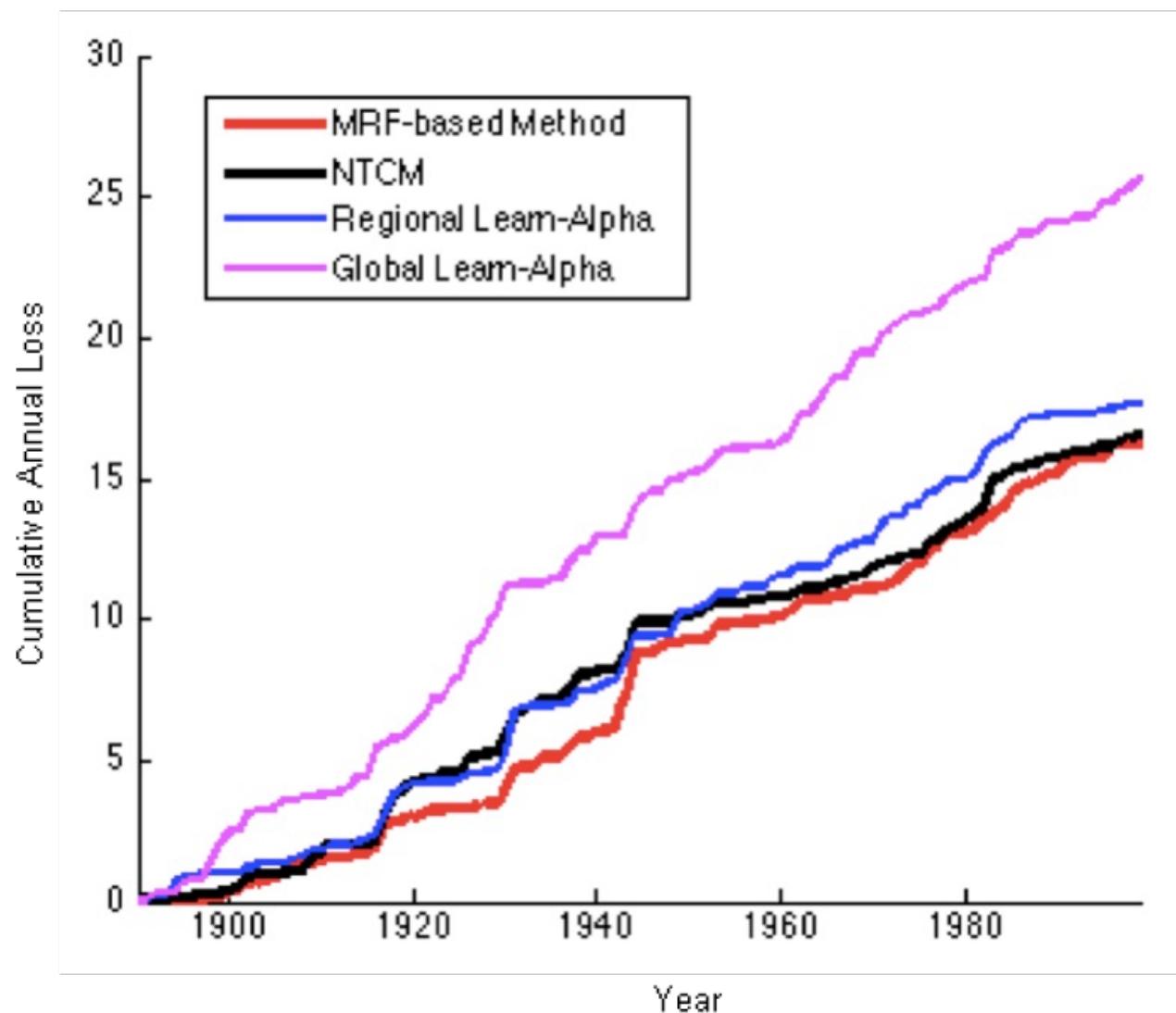
Markov Random Field-based approach



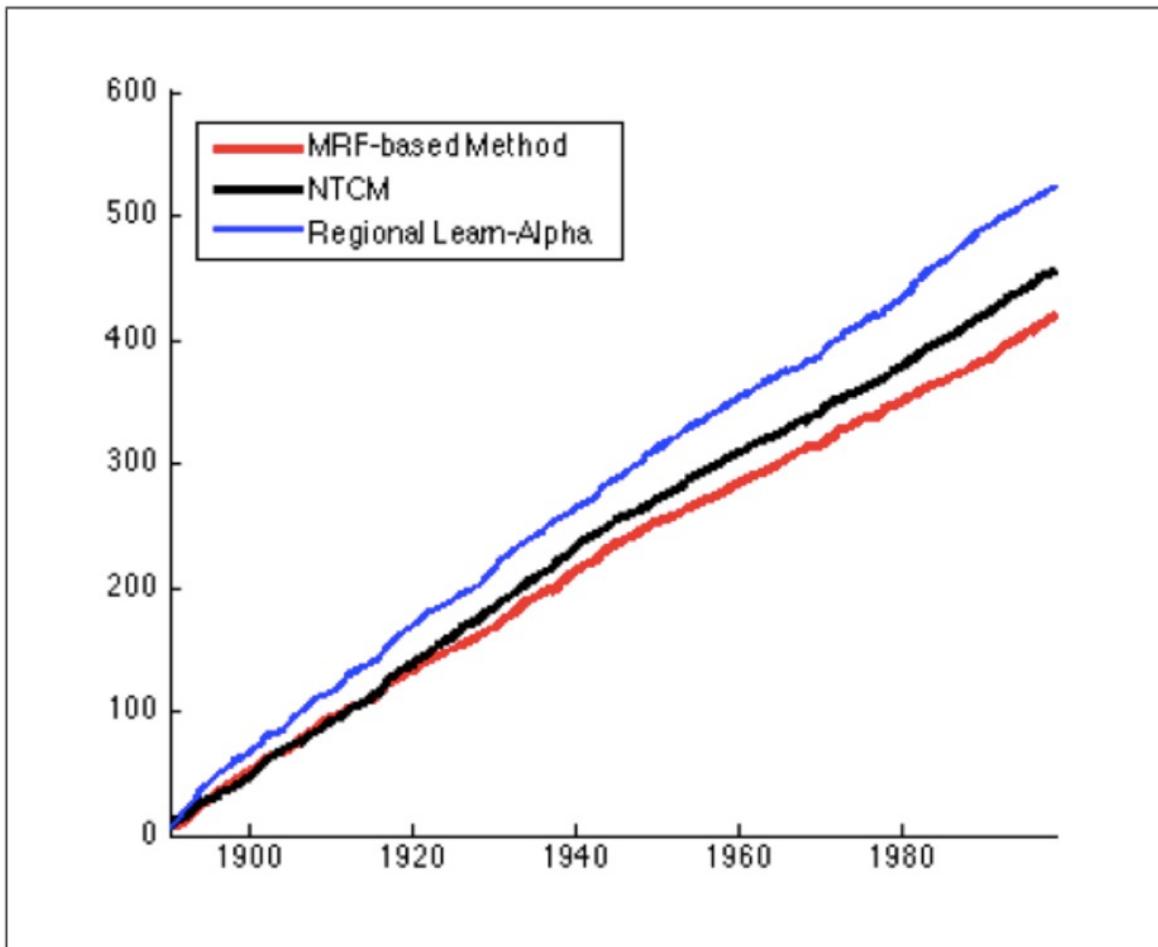
Construct spatial lattice

- Spatial dependencies of same form as temporal dependencies
- Different α_{time} and α_{space} parameters
- Latent variables: best expert at each time and location
- Need to compute marginals

Global prediction loss



Regional prediction loss

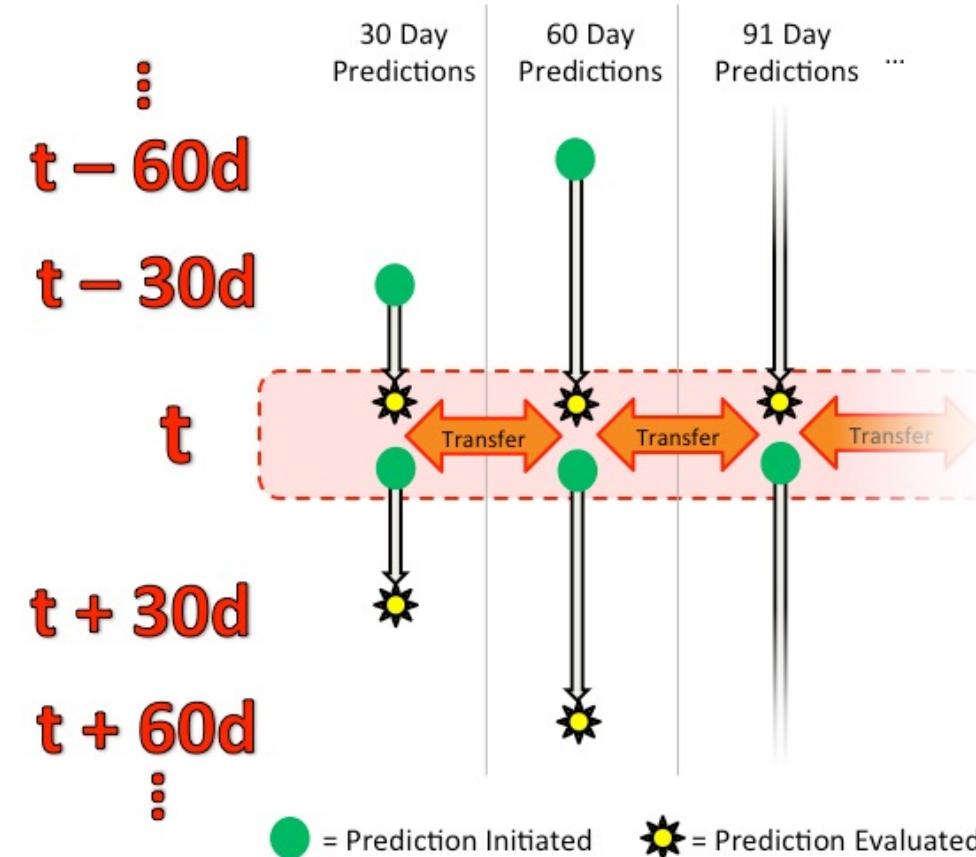


Cumulative mean regional loss of the hindcast.

Seasonal prediction: Online multi-task learning

[McQuade & Monteleoni, Climate Informatics 2015; SIGMOD DSMM 2016]

- Given forecasts of multiple time periods
- Each forecast period treated as a different task
- Allow influence between tasks



Online multi-task learning

Task-similarity matrix [cf. Saha et al., AISTATS 2011]

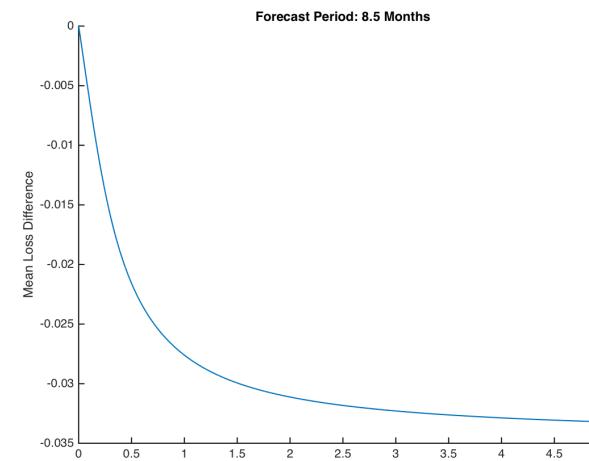
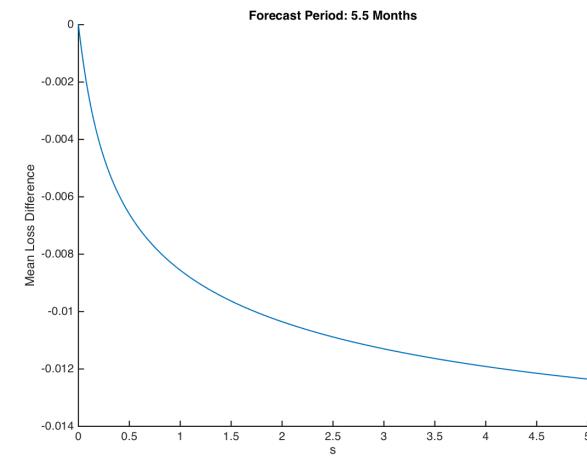
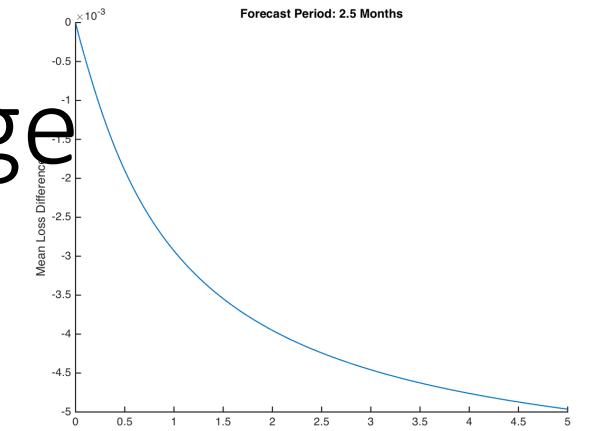
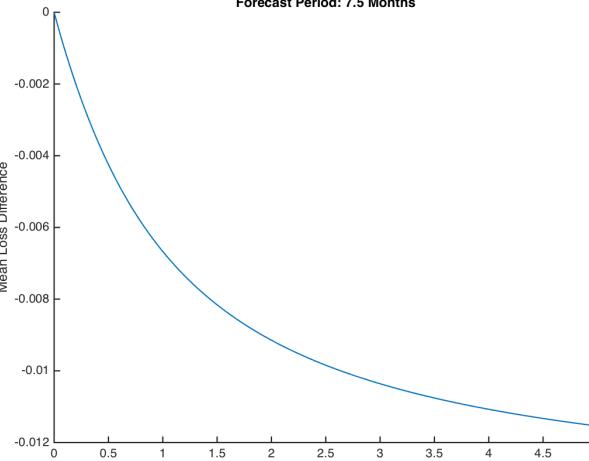
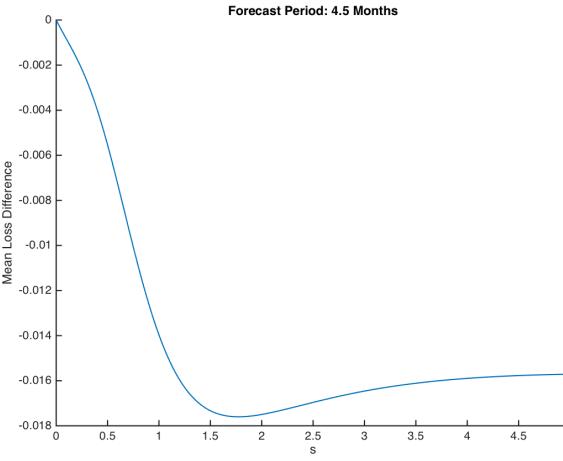
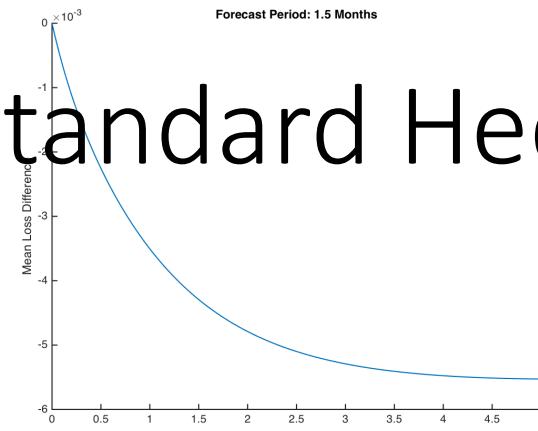
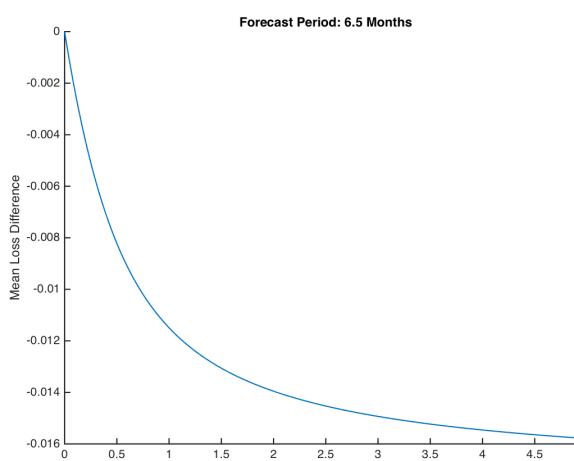
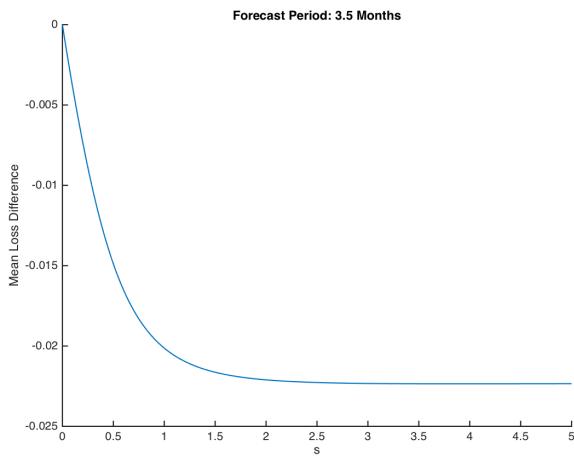
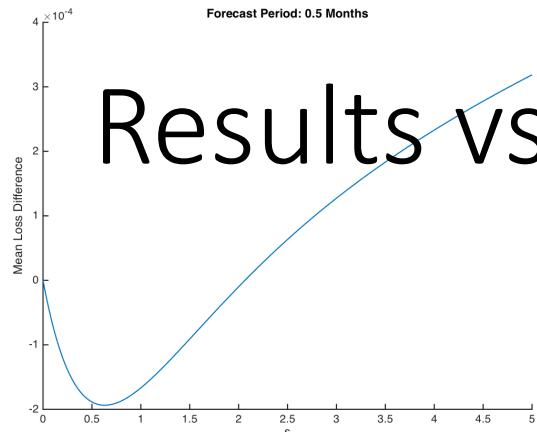
- Allow influence between “neighboring” forecast lengths, parameterized by s

$$S = \begin{matrix} \text{Months:} & 1 & 2 & 3 & 4 & \dots \\ \begin{matrix} 12 \\ 1 \\ 2 \\ \dots \end{matrix} & \left[\begin{matrix} \frac{1}{1+s} & \frac{s}{1+s} & 0 & 0 & \dots \\ 0 & \frac{s}{1+2s} & \frac{1}{1+2s} & \frac{s}{1+2s} & \ddots \\ \vdots & \ddots & \ddots & \ddots & \ddots \\ & & & & \frac{1}{1+s} \end{matrix} \right] \end{matrix}$$

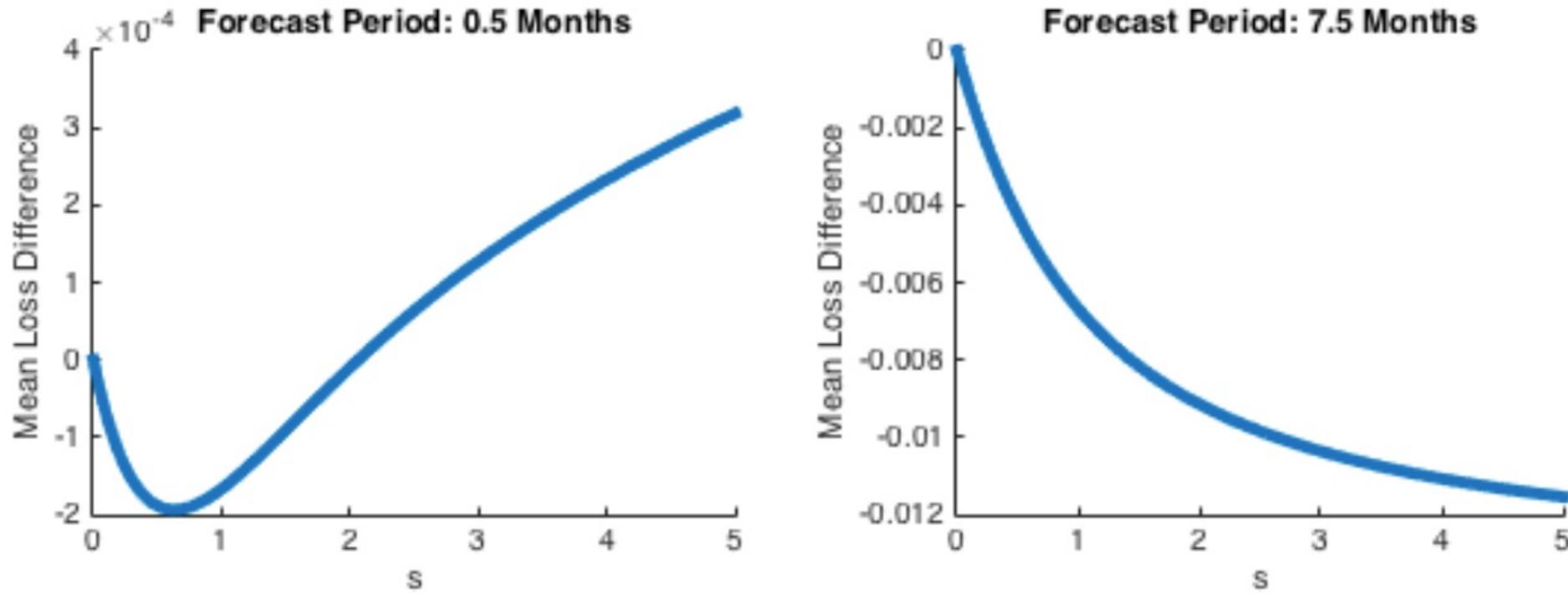
Multi-task update rule (extended from Hedge / Static-Expert algorithm)

$$p_{t+1,j}(i) \propto p_{t,j}(i) e^{-\sum_k S_{j,k} L_{k,t}(i)}$$

Results vs. standard Hedge



Results vs. standard Hedge



For each of the 12 forecast periods, sharing influence from other forecast periods improved predictions.

Only for the 2 forecast periods was loss increased for some s values.

Application to financial volatility prediction [McQuade & M, DSMM 2016]